



# Materials Science

An Indian Journal

Full Paper

MSAIJ, 13(1), 2015 [022-031]

## Studies on the optical properties of ZnO nanostructured thin films synthesized by RF magnetron sputtering

B.Khalfallah\*, F.Chaabouni, M.Abaab

Université Tunis El Manar- ENIT - Laboratoire de Photovoltaïque et Matériaux Semiconducteurs, BP37,

Le belvédère 1002, (TUNIS)

E-mail : bilel\_khalfallah@yahoo.com

### ABSTRACT

Zinc oxide (ZnO) thin films were deposited by RF magnetron sputtering onto glass substrates at room temperature. The thickness effect on the structural, morphological and optical properties of the ZnO films was studied. Films thickness was calculated by interference fringes method and varied from 360 nm to 680 nm. The grain size was in the range of 26 - 29 nm corresponding to nanostructured films. Stress values at different thickness were investigated. The root mean square roughness of the films increased from 3.3 to 12.2 nm in the thickness range of investigation. The average optical transmittance of the films was about 85 % in the visible region. The optical band gap of the ZnO films decrease from 3.37 to 3.09 eV with increasing film thickness. The refractive index dispersion and dielectric constants were investigated by Cauchy, Wemple-Didomenico and Spitzer-Fan models. The results demonstrated that the optical properties were highly related to structural ones. The obtained films can be used as transparent electrodes in solar cells. © 2015 Trade Science Inc. - INDIA

### KEYWORDS

Thin films;  
RF magnetron sputtering;  
Structural properties;  
Optical properties.

### INTRODUCTION

Zinc oxide (ZnO) is wide-band gap semiconductor of 3.37 eV at room temperature a high transparency in the visible range. It is very promising II-VI semiconductor for optoelectronic applications in the UV region, especially for solar cells, gas sensors, acoustic devices, transistors and the production of light emitting devices (LEDs)<sup>[1-4]</sup>. It has a hexagonal wurtzite structure, a natural n-type electrical conductivity and a large exciton binding energy (<“60 meV)<sup>[5,6]</sup>. Several deposition techniques can be used for the production of ZnO thin films, such as laser ablation<sup>[7]</sup>, RF magnetron sput-

tering<sup>[8]</sup>, Spray pyrolysis<sup>[9]</sup> and sol-gel process<sup>[10]</sup>.

In this work, we investigated the effect of the films thickness on the structural, morphological and optical properties of undoped ZnO films produced by RF magnetron sputtering and we showed that the optical and dielectric constants are highly related to the structural properties of the films.

### EXPERIMENTAL DETAILS

#### Fabrication of the ZnO thin films

The ZnO thin films were prepared on amorphous glass substrates at room temperature by RF magnetron

sputtering using a ceramic target of pure ZnO (99.999 %) with a thickness of 5 mm and a diameter of 100 mm. The Glass substrates were used in this study thanks to their low cost, high transparency, high insulating property and low optical absorption above about 300 nm (for ZnO, absorption edge locates at about 360 nm). Before deposition, cleaning of the glass substrates was performed by a soap solution followed by degreasing with acetone in an ultrasonic bath. The substrates were then rinsed properly with de-ionized water and dried in air. The substrates were rotated (15 rd/mn) and placed parallel to the target surface at a distance of 65 mm. RF magnetron sputtering power was adjusted to 200 W. In order to avoid contaminating the films, the chamber was evacuated to a base pressure of about  $10^{-4}$  Pa. Argon gas was introduced into the chamber through a mass flow controller. The mass flow of argon gas was fixed at 2.6 sccm, corresponding to a final pressure of 1.0 Pa. The target was pre-sputtered for 15 min to remove contaminants. ZnO films with different thicknesses were deposited by varying deposition time. The grown samples are represented using the notations E1, E2, E3 and E4 corresponding to a thickness of 360 nm, 485 nm, 575 nm and 680 nm, respectively.

### Characterizations of the produced films

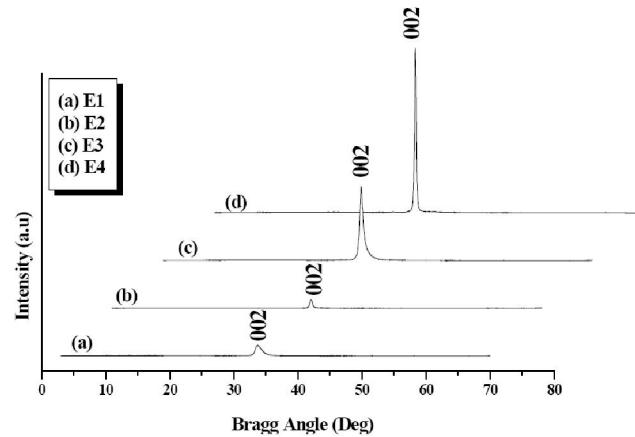
Obtained ZnO films were characterized using X-ray diffraction (PANalytical X'Pert Pro, Philips Co, Ltd) with  $Cu K_{\alpha}$  radiation ( $\lambda = 0.15406$  nm) to identify the crystal structure and orientation of each phase. ASTM table were used for indexing the lines. Film thickness was calculated with Swanepoel procedure<sup>[11]</sup> which is based on the use of the extremes of the interference fringes. Surface morphology was observed using an atomic force microscope (Nanoscope IIIa Veeco type dimension 3100). The optical properties of the films were measured at normal incidence in the wavelength range from 300 to 1800 nm using a double-beam UV-VIS-NIR spectrophotometer (Shimadzu).

## RESULTS AND DISCUSSION

### Structure characterization

Figure 1 shows the XRD patterns of ZnO films deposited at different thicknesses. All samples exhibit a (0 0 2) peak at  $2\theta < 34^\circ$ , indicating that the RF

sputtered ZnO films have a hexagonal wurtzite structure and show a good c-axis orientation perpendicular to the substrate. The c-axis orientation in ZnO films can be explained by the model proposed by Drift<sup>[12]</sup>. According to this model, nucleation with various orientations can be formed at the initial stage of the film deposition and each nucleus competes to grow; but only nuclei having the fastest growth rate on the substrate can survive, i.e., c-axis orientation is achieved. The absence of additional peaks in the XRD patterns excludes the possibility of any extra phases and/or large size precipitates in the films. The (0 0 2) ZnO peak intensity increases as the film thickness increases from E1 (360 nm) to E4 (680 nm).



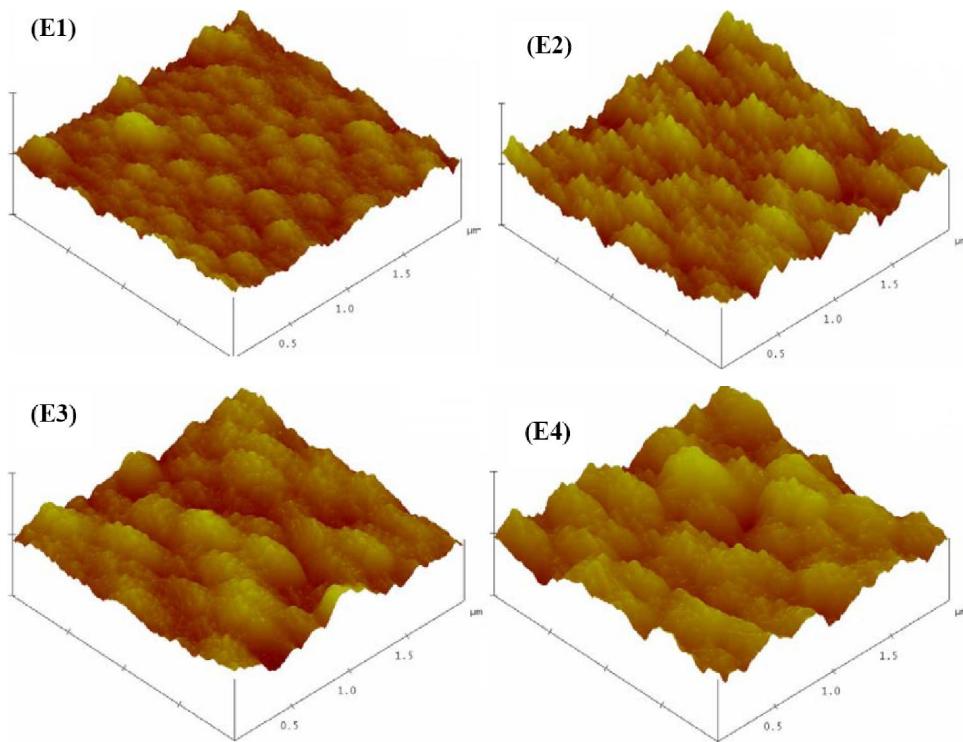
**Figure 1 : XRD patterns of ZnO films deposited on glass substrates at different film thicknesses**

To assess the crystal quality of ZnO films, the grain size as a function of film thickness was calculated from XRD data by Scherrer formula<sup>[13]</sup>:

$$D = \frac{0.9\lambda}{B \cos \theta} \quad (1)$$

where  $D$  is the average grain size,  $\lambda$  is the X-ray wavelength,  $\theta$  is the diffraction angle of the peak and  $B$  is the value of the full width at half maximum (FWHM) of the (002) peak. As film thickness increases, the FWHM decreases from 0.32 to 0.29 and the grain size increases from 26 to 29 nm indicating an enhancement of the crystallinity. Similar behavior was reported by W.L. Dang et al.<sup>[14]</sup> and C. S. Baek et al.<sup>[15]</sup>.

The strain  $\varepsilon$  in ZnO thin films along c-axis perpendicular to the substrate was calculated using the equation:



**Figure 2 : AFM images of ZnO films at different films thickness (Surface area studied = 2 × 2 μm<sup>2</sup>)**

$$\varepsilon(\%) = \frac{\Delta c}{c_0} \times 100\% \quad (2)$$

where  $\Delta c$  is the difference between the lattice parameter ‘ $c$ ’ of the films (calculated from XRD data) and the lattice parameter ‘ $c_0$ ’ of unstrained ZnO (5.206 Å)<sup>[16]</sup>. For hexagonal systems, the residual stress  $\sigma$  in the plane of the film can be calculated from the strain (see Eq. (3)) with the biaxial strain model<sup>[16]</sup>:

$$\sigma = 2C_{13} - \frac{C_{33}(C_{11} + C_{12})}{C_{13}} \times \varepsilon \quad (3)$$

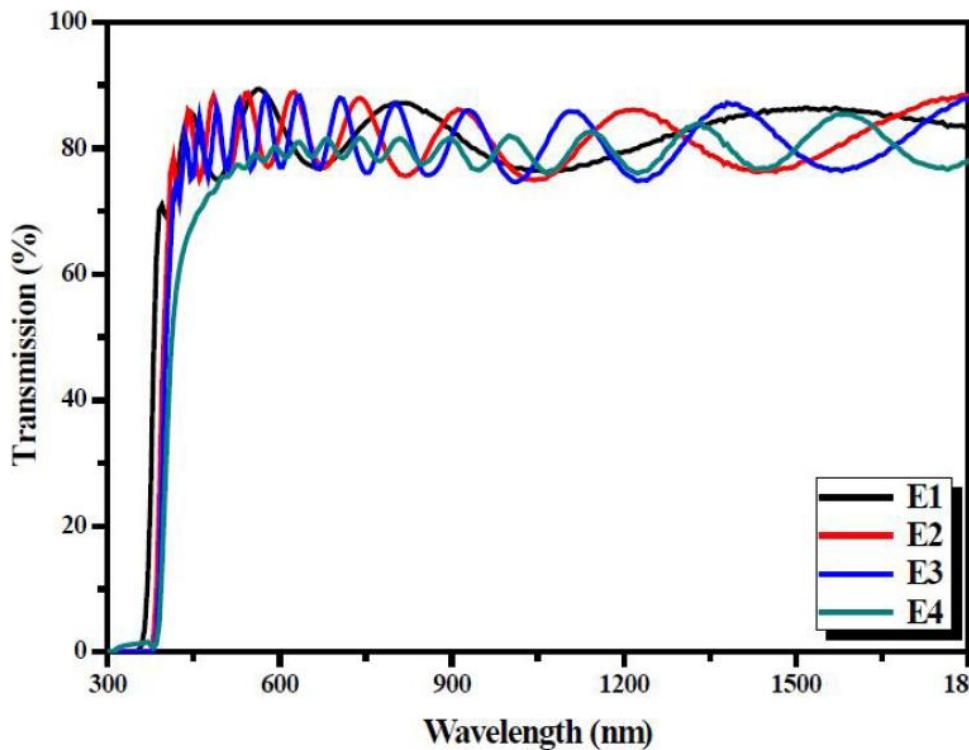
where  $C_{ij}$  are the elastic stiffness constants for single ZnO crystal ( $C_{11} = 208.8$  GPa,  $C_{33} = 213.8$  GPa,  $C_{12} = 119.7$  GPa,  $C_{13} = 104.2$  GPa)<sup>[17,18]</sup>. The estimated values of stress  $\sigma$  in the grown films are found to decrease from -4.74 to -0.09 GPa with films thickness. The negative stress values indicate that the films are in a state of compressive intrinsic stress<sup>[19,20]</sup>. The intrinsic stress originates from defects in the films and is thought to be associated with the sputtered particles bombarding the grown film during sputtering process, which will cause lattice distortion of the films to increase the stress<sup>[21]</sup>.

### Morphological characterization

Figure 2 displays the AFM micrographs (2 μm × 2 μm) of the ZnO films with various thicknesses. It can be seen that all samples demonstrate a uniform and densely packed granular arrangement. The crystallite diameter measured using AFM analysis is around 19, 33, 50 and 65 nm for E1, E2, E3 and E4, respectively. The grain size estimated by XRD data and the crystallite size indicating by AFM vary in the same trend indicating that crystallite is composed of small grains surrounded by the grain boundaries. The RMS roughness is gradually increased from 3.30 to 12.23 nm with film thickness. This increase may be related to the larger grain size formation as well as an increase in the grain film porosity<sup>[22]</sup>. Such an increase of RMS roughness with increasing film thickness was also noticed by R. S. Reddy et al.<sup>[23]</sup>. The increase of RMS roughness of ZnO films leads significant effect on the industrial applications such as gas sensors.

### Optical characterization

Figure 3 shows the transmittance ( $T$ ) spectra in the wave range of 300 – 1800 nm of the ZnO films with different thicknesses. All the spectra reveal very pronounced interference effects in the transparency and NIR regions (400 - 1800 nm) with a sharp fall of trans-



**Figure 3 : Optical transmittance spectra of ZnO at different films thickness**

mittance at the band edge. All the films are highly transparent with transmittance values in the range of 75 - 90 %. In addition, the reflectance values for all the samples are in the range of 10 - 25 %. This result suggests that these films behave as a transparent material and indicate a good optical quality due to the low absorption losses in the visible and NIR range. Hence, these films can be used as transparent window materials in many optoelectronic devices.

The absorption coefficient of the ZnO films is evaluated from the transmittance ( $T$ ) and reflectance ( $R$ ) data by using the following formula<sup>[24]</sup>:

$$\alpha = \frac{1}{d} \ln \left[ \frac{(1-R)^2}{T} \right] (\text{cm}^{-1}) \quad (4)$$

where  $\alpha$  is the absorption coefficient,  $d$  is the film thickness and  $R$  and  $T$  are the reflection and transmission coefficients, respectively.

Figure 4 shows the dependence of the absorption coefficient on wavelengths for the ZnO films with different thicknesses. It can be seen that all the samples have relatively high absorption coefficients (higher than  $10^5 \text{ cm}^{-1}$  in the UV region). Similar behavior was reported

by N. Ekemet *et al.*<sup>[25]</sup>. This result reveals that these films have potential in photovoltaic applications<sup>[26]</sup>. Furthermore, the strong absorption region extends until smaller wavelengths which belong to the UV region. So, these films are also promising materials for solar protective coatings<sup>[27-29]</sup>.

The optical band gap  $E_g$  of the films can be determined from the absorption coefficient of the films using the relation for parabolic bands<sup>[30]</sup>:

$$(\alpha h\nu)^2 = A(h\nu - E_g^{opt}) \quad (5)$$

where,  $h\nu$  is the photon energy,  $A$  is constant and  $E_g$  is the optical band gap. The values of the direct optical band gaps are obtained by plotting  $(\alpha h\nu)^2$  as a function of  $h\nu$  and extrapolating the linear portion of the curve to the energy ( $h\nu$ ) axis.  $(h\nu)^2$  versus  $h\nu$  for the deposited ZnO films are presented in Figure 5. The optical band gap values of the deposited ZnO films are found to decrease from 3.37 to 3.09 eV with film thickness.

The decrease in bandgap values with increasing the films thickness (see Figure 6) can be explained with the relaxation of the compressive stress due to longer cycle times as reported by T. Singh *et al.*<sup>[31]</sup>. Indeed, the compressed lattice is expected to provide a wider bandgap

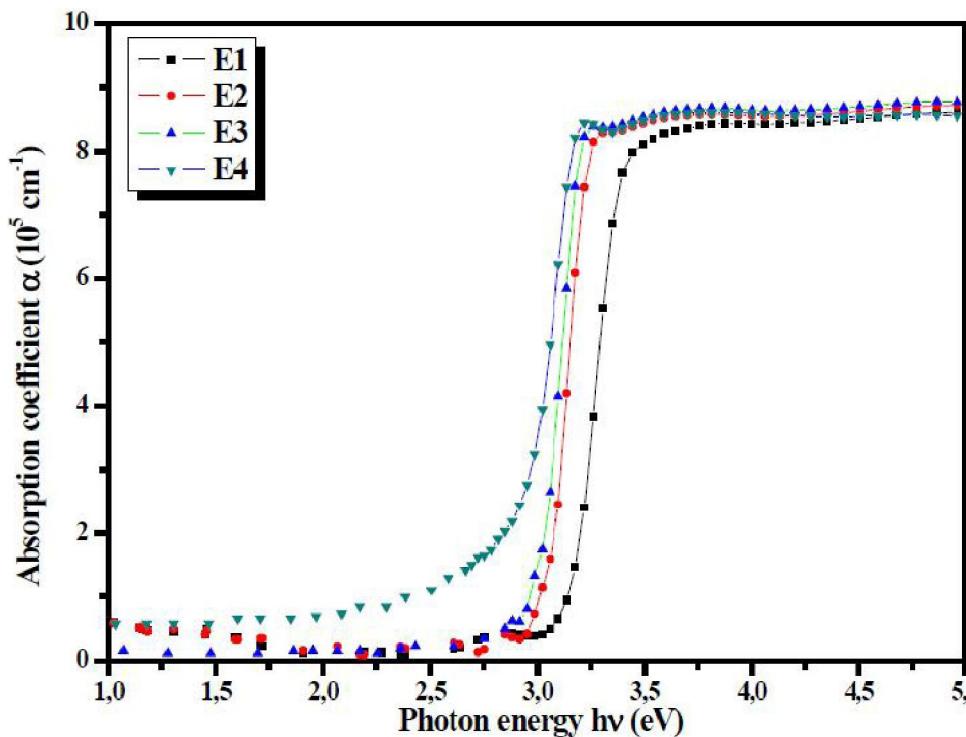
**Full Paper**

Figure 4 : Absorption coefficient of ZnOat different films thickness

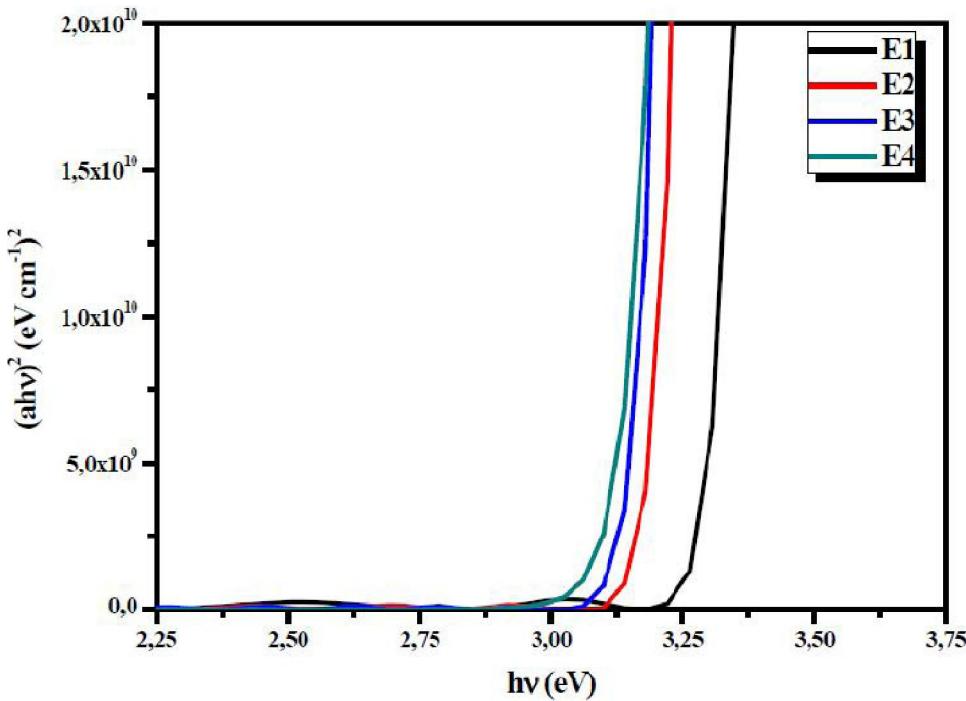


Figure 5 : The Tauc plots of ZnO at different films thickness

because of the increased repulsion between the oxygen  $2\ p$  and the zinc  $4s$  bands<sup>[32]</sup>.

The refractive index  $n(\lambda)$  can be determined using the transmission envelopes of thin films deposited on a transparent substrate<sup>[33]</sup>. Using this method, the refractive index is expressed by<sup>[34]</sup>.

$$n = \left[ N + (N^2 - S^2)^{1/2} \right]^{1/2} \quad (6)$$

Where

$$N = 2S \frac{T_M - T_m}{T_M T_m} + \frac{S^2 + 1}{2} \quad (7)$$

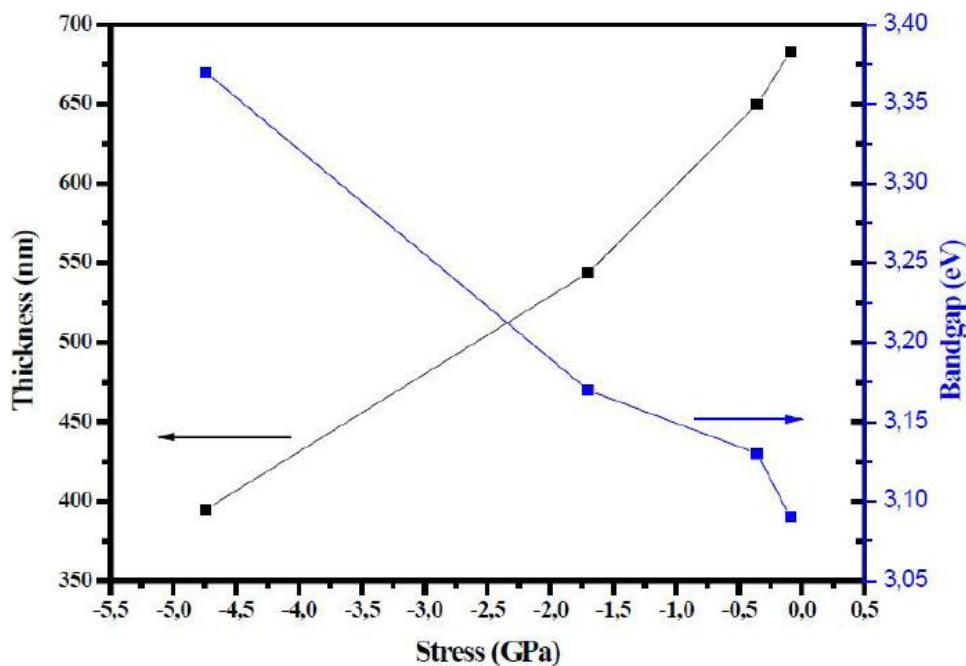


Figure 6 : Stress evolution in ZnO thin films with increasing thickness and bandgap evolution in ZnO thin films with decreasing stress

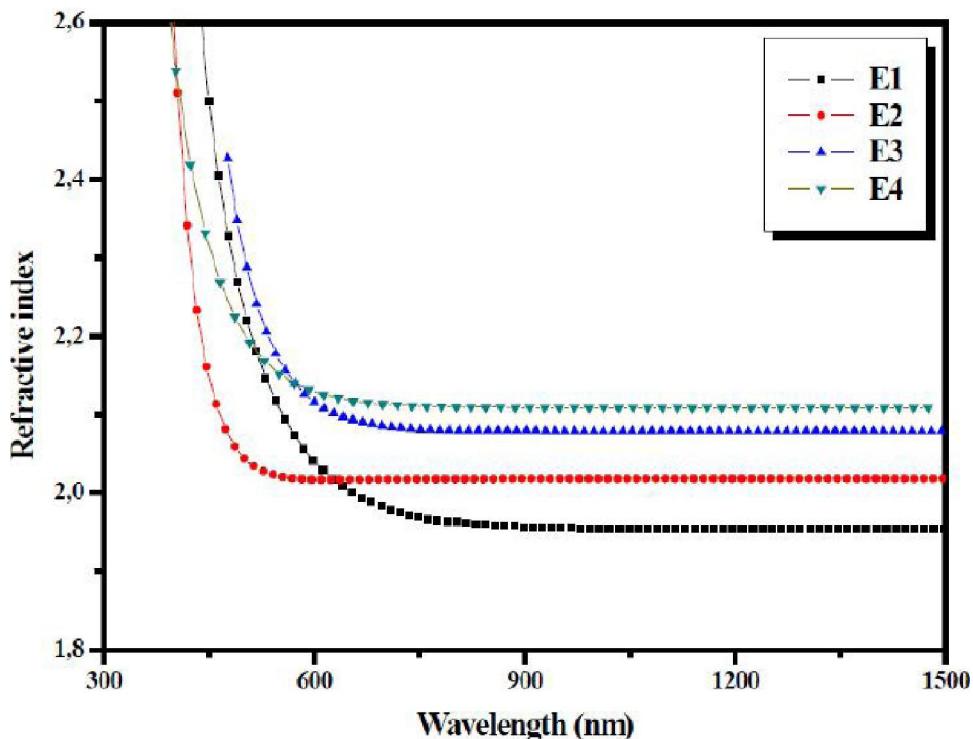


Figure 7 : Refractive index versus wavelength  $\lambda$  of ZnO at different films thickness

where  $S$  is the refractive index of the glass substrate.  $T_m$  and  $T_M$  are the envelope values at maximum and minimum positions of the transmission spectra, respectively. Figure 7 shows the refractive index evolution as a function of wavelength. It's clear that the refractive index values decrease sharply in the range of 400 –

750 nm than stabilize in the range of 750 – 1500 nm. The refractive indexes for all samples are found to increase by increasing film thicknesses. This result may be due to the increase in the values of grain size and the improvement in the crystallinity indicating an improvement in films density. With the increase of film thick-

## Full Paper

ness, the film becomes denser and denser.  $n(\lambda)$  of the deposited ZnO thin films are fitted by the Cauchy model<sup>[35]</sup>:

$$n(\lambda) = n_0 + \frac{A}{\lambda^2} + \frac{B}{\lambda^4} + \frac{C}{\lambda^6} \quad (8)$$

where  $n_{0,c}$ , A, B and C are the Cauchy's parameters and  $\lambda$  is the wavelength of the light used. The good fit implies that the films have normal dispersion for the entire studied wavelength range. The estimated values of  $n_{0,c}$ , A, B and C evaluated from the fitting of  $n(\lambda)$  by the Cauchy formula are tabulated in TABLE 1.

The single oscillator Wemple–Didomenico<sup>[36,37]</sup> was also used to fit the dispersion of refractive index as:

$$n^2(hv) = 1 + \frac{E_d E_0}{E_0^2 - (hv)^2} \quad (9)$$

where  $hv$  is the photon energy,  $E_0$  is the single oscillator energy which is a measure of the energy difference between the 'centres of gravity' of the valence and conduction bands and an indicator for the energy gap quantification of the material<sup>[38]</sup> and  $E_d$  is the dispersion energy which represents a measure of the average strength of interband optical transitions. Figure 8 shows plots of  $(n^2 - 1)^{-1}$  versus  $(hv)^2$  and by fitting a straight line,  $E_0$  and  $E_d$  can be determined directly from slope,  $(E_0 E_d)^{-1}$  and the intercept  $E_0/E_d$  on the vertical axis. The refractive index  $n_{0,w}$  can also be deduced from the dispersion relationship for  $(hv) > 0$ , extrapolated from the Wemple–Didomenico single oscillator fit.

The estimated values of  $n_{0,w}$ ,  $E_0$  and  $E_d$  at different films thickness were grouped in TABLE 1. We note that the values of  $n_0$  found by the Cauchy fitting and the Wemple–DiDomenico model are in good agreement.

Under the same model, the refractive index can also be analyzed to determine the long wavelength refractive index  $n_\infty$ , average oscillator wavelength  $\lambda_0$  and oscillator length strength  $S_0$  of each thin film. These values can be obtained by using the following relations<sup>[39,40]</sup>:

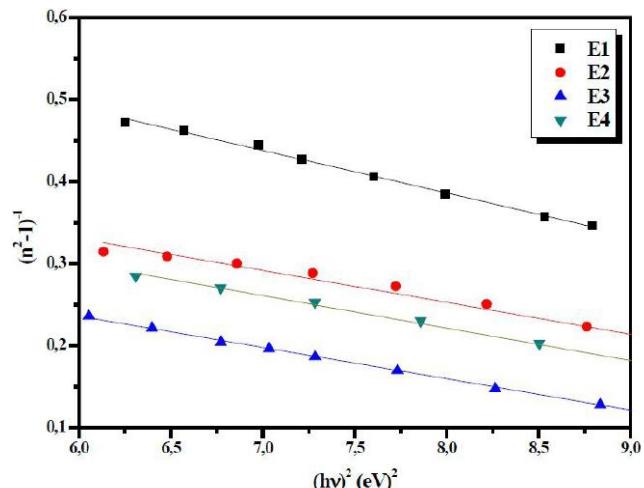


Figure 8 : Plot of  $(n^2 - 1)^{-1}$  versus  $(hv)^2$  of ZnO at different films thickness for the determination of  $n_0, n_\infty, S_0$ ,  $E_0$  and  $E_d$

TABLE 1 : Calculated values of Cauchy parameters  $n_0, A$ , Band C

$n_{0,c}$	$A (10^5 \text{ nm}^2)$	$B (10^{10} \text{ nm}^4)$	$C (10^5 \text{ nm}^6)$
1	1.81	0.218	-1.72
E2	1.94	1.340	-7.76
E3	2.04	0.941	-6.70
E4	2.11	1.553	-10.77

$$\frac{n_\infty^2 - 1}{n^2 - 1} = 1 - \left( \frac{\lambda_0}{\lambda} \right)^2 \quad (10)$$

$$n_\infty^2 = 1 + S_0 \lambda_0^2 \quad (11)$$

$$n^2 - 1 = \frac{S_0 \lambda_0^2}{1 - \left( \frac{\lambda_0}{\lambda} \right)^2} \quad (12)$$

From Figure 8, we obtain  $n_\infty$  and  $\lambda_0$  values from the linear part of  $1/(n^2 - 1)$  versus  $\lambda^2$  curve. These values are summarized in TABLE 2.

Using the Spitzer–Fan model<sup>[41]</sup>, certain dielectric constants which are linked to the refractive index  $n(\lambda)$ , are determined allowing better analyze of

TABLE 2 : Calculated values of wemple–Didomenico parameters

	$E_g (\text{eV})$	$E_0 (\text{eV})$	$E_d (\text{eV})$	$n_{0,w}$	$S_0 (\mu\text{m}^{-2})$	$\lambda_0 (\mu\text{m})$	$n_\infty$
E1	3,37	5,73	14,85	1.77	55,28	0,21	1,75
E2	3,17	4,51	10,28	1.90	29,20	0,27	1,80
E3	3,13	3,85	9,95	2.03	26,70	0,28	1,85
E4	3,09	3,95	8,50	2.15	17,45	0,35	1,90

**TABLE 3 : Calculated values of dielectric constants (spitzer-fan model)**

	$\epsilon_{\infty}$	$-4\pi\chi_e$	$N/m^* (10^{49} \text{ g}^{-1} \text{ cm}^{-3})$
E1	7.55	1-16.72	7.16
E2	4.95	0.47-9.87	3.63
E3	4.75	0.43-7.93	2.83
E4	5.00	0.21-4.55	1.52

the optical properties of the thin films.

$$\epsilon_r = n^2 - k^2 = \epsilon_{\infty} - [e^2 / \pi c^2] (N / m^*) \lambda^2 \quad (14)$$

$$[e^2 / \pi c^2] (N / m^*) \lambda^2 = -4\pi\chi_e \quad (15)$$

where  $\epsilon_{\infty}$  is the high-frequency dielectric constant in the absence of any contribution from free carrier,  $k$  is the

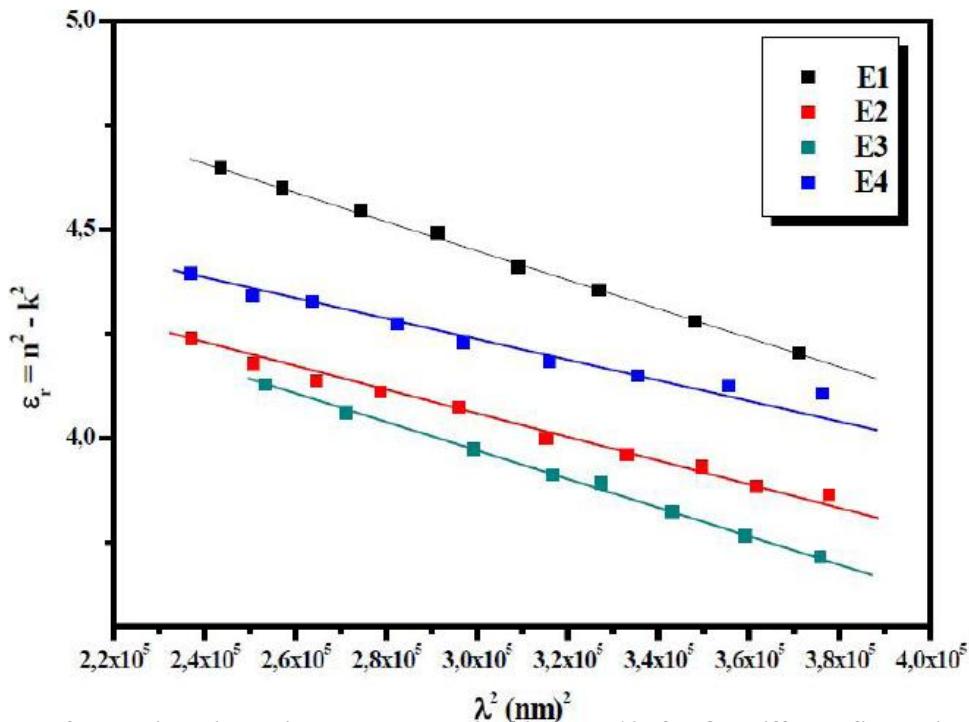


Figure 9 : Plot of the optical dielectric constant  $\epsilon_r = n^2 - k^2$  versus  $\lambda^2$  of ZnO at different film thicknesses

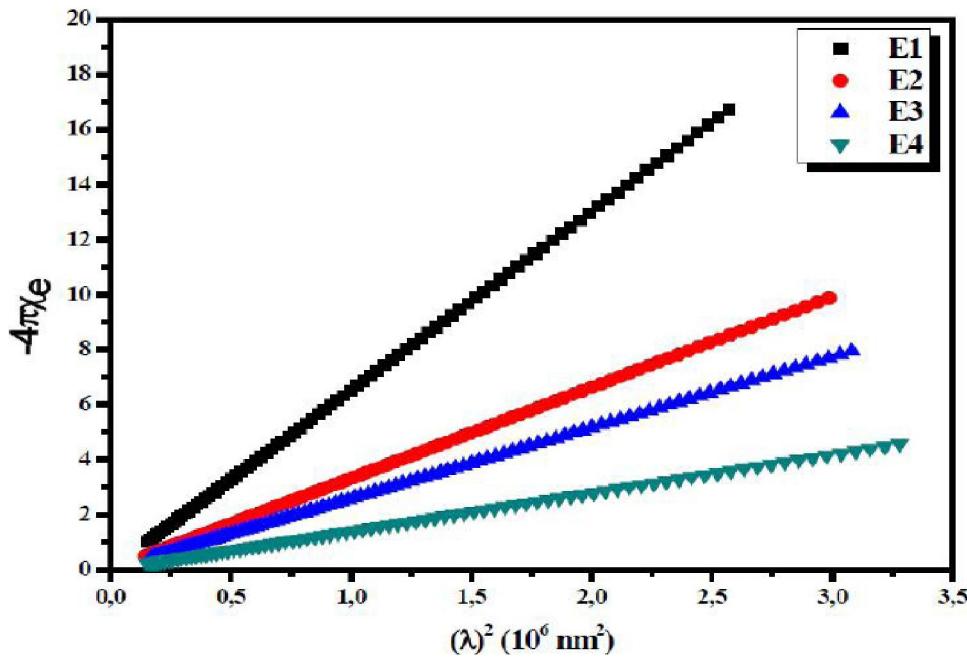


Figure 10 : Plot of ( $-4\pi\chi_e$ ) versus  $\lambda^2$  of ZnO at different film thicknesses

## Full Paper

extinction coefficient,  $\chi_e$  is the electric free carrier susceptibility,  $N/m^*$  is the carrier concentration to the effective mass ratio,  $e$  is the electronic charge and  $c$  is the velocity of light. The values of  $N/m^*$  and  $\epsilon_r$  were estimated by plotting  $\epsilon_r$  versus  $\lambda^2$  (Figure 9) and summarized in TABLE 3.

Figure 10 shows ( $4\pi\chi_e$ ) versus  $\lambda^2$ . The figure depicts that  $\chi_e$  increases in magnitude with the wavelength and becomes sufficiently large to reduce the refractive index and the dielectric constant in the near-infrared region. A good fit to a straight line is seen from which the free carrier susceptibility values at the extremes of the investigated range were estimated.

## CONCLUSIONS

In conclusion, we have studied the effect of the thickness on the structural, morphological and optical properties of the ZnO thin films prepared by RF magnetron sputtering. All the samples have a typical hexagonal wurtzite structure with a smooth surface and a growth in a preferred orientation along the direction (002). AFM images showed that the grain size and surface RMS roughness are obviously influenced by the ZnO film thickness. Grain size and RMS roughness increased with increasing thickness. The optical transmittance of ZnO films was over 80 % in the visible region, and red-shift of the optical absorption edge was observed. The optical band gap decreased from 3.37 eV to 3.09 eV with increasing thickness from 360 to 680 nm. We used the models of Cauchy, Wemple–Didomenico and Spitzer–Fan for the analysis of the dispersion of the refractive index and the determination of the optical and dielectric constants. These studies show that ZnO has excellent optical properties for solar cell applications as antireflection coating.

## REFERENCES

- [1] R.Ebrahimifard, M.R.Golobostanfar, H.Abdizadeh; Applied Surface Science, **290**, 252–259 (2014).
- [2] R.Vettumperumal, S.Kalyanaraman, R.Thangavel; Journal of Molecular Structure, **1059**, 61–67 (2014).
- [3] Y.E.Jeong, S.Park; Current Applied Physics, **14**, 30-33 (2014).
- [4] R.Sridhar, C.Manoharan, S.Ramalingam, S.Dhanapandian, M.Bououdina; Spectrochimica Acta Part A: Molecular and Biomolecular Spectroscopy, **120**, 297–303 (2014).
- [5] L.Ma, X.Ai, X.Huang, S.Ma; Superlattices Microstruct., **50**, 703–712 (2011).
- [6] C.F.Wang, B.Hub, H.H.Yia; Optik, **123**, 1040–1043 (2012).
- [7] E.Fazio, A.M.Mezzasalma, G.Mondio, T.Serafino, F.Barreca, F.Caridi; Appl.Surf.Sci., **257**, 2298–2302 (2011).
- [8] F.Gao, X.Y.Liu, L.Y.Zheng, M.X.Li, Y.M.Bai, J.Xie; J.Cryst.Growth, **371**, 126–129 (2013).
- [9] S.Benramache, B.Benhaoua; Superlattices Microstruct., **52**, 1062–1070 (2012).
- [10] P.Jongnavakit, P.Amornpitoksuk, S.Swanboon, T.Ratana; Thin Solid Films, **520**, 5561–5567 (2012).
- [11] R.Swanepoel; J.Phys., **16**, 1214 (1983).
- [12] V.A.Drift; Philips Res.Rep., **22**, 267 (1967).
- [13] B.E.Warren; X-ray Diffraction, Dover, New York (1990).
- [14] W.L.Dang, Y.Q.Fu, J.K.Luo, A.J.Flewitt, W.I.Milne; Superlattices and Microstructures, **42**, 89–93 (2007).
- [15] C.S.Baek, D.H.Kim, H.H.Kim, K.J.Lim; Journal of Ceramic Processing Research., **132**, 403-406 (2012).
- [16] H.C.Ong, A.X.E.Zhu, G.T.Du; Appl.Phys.Lett., **80**, 941–943 (2002).
- [17] B.D.Cullity, S.R.Stock; Elements of X-ray Diffractons, 3, Prentice Hall, Engle-wood Cliffs, NJ, (2001).
- [18] R.Kumar, N.Khare, V.Kumar, G.L.Bhalla; Appl.Surf.Sci., **254**, 6509–6513 (2012).
- [19] R.Kumar, N.Khare, V.Kumar, G.L.Bhalla; Applied Surface Science, **254**, 6509–6513 (2008).
- [20] T.Singh, T.Lehnen, T.Leuning, D.Sahu, S.Mathur; Applied Surface Science, **289**, 27–32 (2014).
- [21] B.L.Zhu, S.J.Zhu, J.Wang, J.Wua, D.W.Zeng, C.S.Xie; Physica E, **43**, 1738–1745 (2011).
- [22] N.Kakani, S.H.Jee, S.H.Kim, J.Y.Oh, Y.S.Yoon; Thin Solid Films, **519**, 494 (2010).
- [23] R.S.Reddy, A.Sreedhar, A.Sivasankar Reddy, S.Uthanna; Adv.Mat.Lett., **3**, 239-245 (2012).
- [24] D.E.Milovzorov, A.M.Ali, T.Inokuma, Y.Kurata, T.Suzuki, S.Hasegawa; Thin Solid Films, **382**, 47 (2001).
- [25] N.Ekem, S.Korkmaz, S.Pata, M.Z.Balbag, E.N.Cetin, M.Ozmumcu; international journal of hydrogen energy, **34**, 5218–5222 (2009).

- [26] C.Bauer, G.Boschloo, E.Mukhtar, A.Hagfeldt; *Chem.Phys.Lett.*, **387**, 176–181 (2004).
- [27] S.S.Shariffudin, M.Salina, S.H.Herman; *Transactions On Electrical And Electronic Materials*, **13**, 102-105 (2012).
- [28] L.Miao, S.Tanemura, M.Tanemura, S.P.Lau, B.K.Tay; *J.Mater.Sci.Mater.Electron.*, **18**, 343–346 (2007).
- [29] G.X.Liang, P.Fan, X.M.Cai, D.P.Zhang, Z.H.Zheng; *Journal Of Electronic Materials*, **40** (2011).
- [30] J.I.Pankove; *Optical Processes in Semiconductors*, Dover, New York (1971).
- [31] T.Singh, T.Lehnen, T.Leuning, D.Sahu, S.Mathur; *Applied Surface Science*, **289**, 27– 32 (2014).
- [32] R.Ghosh, D.Basak, S.Fujihara; *J.Appl.Phys.*, **96**, 2689–2692 (2004).
- [33] E.Marquez, J.B.Ramirez-Malo, P.Villares, R.Jimenez-Garay, R.Swanepoel; *Thin Solid Films*, **254**, 83 (1995).
- [34] R.Swanepoel; *Journal of Physics E: Scientific Instruments*, **17**, 896 (1984).
- [35] H.G.Tompkins, W.A.McGahan; *Spectroscopic Ellipsometry and Reflectometry*, John Wiley & Sons Inc. (1999).
- [36] S.H.Wemple, M.Di Domenico; *Phys.Rev.B*, **143**, 1338 (1971).
- [37] S.H.Wemple; *Phys.Rev.B*, **7**, 3767 (1973).
- [38] F.Skuban, S.R.Lukic, D.M.Petrovic, I.O.Gúth; *Journal of Non-Crystalline Solids*, **355**, 2059–2062 (2009).
- [39] A.K.Wolaton, T.S.Moss; *Proc.R.Soc.A*, **81**, 5091 (1963).
- [40] P.A.Lee, G.Said, R.Davis, T.H.Lim; *J.Phys.Chem.Solids*, **30**, 2719–2729 (1969).
- [41] W.G.Spitzer, H.Y.Fan; *Phys.Rev.*, **106**, 882 (1957).