

# Prediction of the solid solubility in supercritical carbon dioxide using a new mixing rule with Lenard-Jones parameters 

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## ABSTRACT

This study is performed to provide a new mixing rule based on the LenardJones parameters for calculation of the solid solubility in supercritical carbon dioxide. The solubility of solid solutes in supercritical fluid is an important thermo-physical property which is required to be determined. Since generally there are few data about solubility, we need to provide methods to estimate the solubility of solid solutes in supercritical solvents by using limited information. In the current study, the cubic PengRobinson (PR) and Soave-Redlich-Kwong (SRK) equations of state are used to estimate the solid solubilities of 18 solutes in supercritical carbon dioxide. This estimation is performed by using four mixing rules which are called the van der waals one fluid rule with one (VDW1) and two (VDW2) adjustable parameters, the covolume dependent (CVD) rule and the new mixing rule. The prediction of the new mixing rule is more accurate than the other mixing rules in the same equations of state for calculating solid solubility in supercritical carbon dioxide and the results of various calculations demonstrate that the proposed mixing rule is in good agreement with the 665 experimental data points that are used in this work. © 2013 Trade Science Inc. - INDIA

## KEYWORDS

Mixing rule; Equation of state; Solid solubility; Supercritical carbon dioxide; Lenard-Jones parameters.

## INTRODUCTION

Supercritical fluids (SCF) are widely used in chemical processes such as extractions, purifications, separations, crystalgrowth, reactions, fractionations, remove impurity of chemical products, regenerating activated carbon, industrial food applications and many other processes ${ }^{[1]}$. Carbon dioxide is a promising solvent since it is inexpensive, nontoxic, inflammable, and environmentally acceptable while it possesses a low critical temperature and a moderate critical pressure $\left(\mathrm{T}_{\mathrm{C}}=304.25\right.$

K and $\mathrm{P}_{\mathrm{C}}=73.8$ bar $)^{[1,2]}$.
The design of the extraction processes with SCF's depends upon the ability to predict the solubility of solid in supercritical fluids ${ }^{[2]}$. In order to design optimized supercritical processes, solubility data of the considered compounds are needed. It is difficult to determine solid solubility in supercritical fluid accurately. Due to the difficulties of experimental measurements and also time-consuming and costly nature of such techniques ${ }^{[3]}$, it is desirable to develop predictive methods for estimating the phase behavior of these kinds of systems.

To predict the solubility of a solute in supercritical fluids,Equation of State (EOS) models are widely incorporated.Cubic EOS's are the simplest equations capable of predicting and representing fluid phase equilibrium of pure and fluid mixtures ${ }^{[2]}$. Therefore thermodynamic models including EOS's with different mixing rules are widely used to predict solid solubilities atequilibrium conditions.A number of empirical mixing rules have been proposed for the representation of solidsupercritical fluid equilibrium, which have been discussed in reviews by Johnston et al. ${ }^{[4]}$ and Brennecke and Eckert ${ }^{[5]}$. Several researchers have suggested that the selection of the mixing rules is more important than the EOS itself ${ }^{[6,7]}$. Therefore, the focus of this study is to propose a new mixing rule for the determination of the solid solubilities of aromatic hydrocarbons, aliphatic carboxylic acids, aromatic acids, and heavy aliphatic and aromatic alcohols in supercritical carbon dioxide. The cubic Peng-Robinson (PR) ${ }^{[8]}$ and Soave-RedlichKwong (SRK) ${ }^{[9]}$ equations of state have been used to calculate the solid solubilities of 18 solutes in supercritical $\mathrm{CO}_{2}$, by using four mixing rules, namely, the the van derWaals one fluid rule with one (VDW1) and two (VDW2) adjustable parameters, the covolume dependent (CVD) rule and the new mixing rule.

In the new mixing rule, the surface of solid is considered as a plate that is surrounded by molecules of supercritical carbon dioxide; then the interaction energy of sorbent molecule with a single infinite layer plane of solid molecule is calculated using Kirkwood-Müller formula and distance between the layers is related on diameters of molecule and then a volume correction term is proposed on the basis of second virial coefficient and Lenard-Jones 6-12 potential.

The model is applied to calculate solubilities of various solid compounds in supercritical $\mathrm{CO}_{2}$. The optimal values of the model adjustable parameters have been obtained for 665 experimental data points. Finally, the most accurate combination of the mentioned equations of state with the mixing rules, which leads to the least absolute average deviation of the results from experimental values (AARD \%) is reported.

## CALCULATION OF SOLUBILITY OF SOLIDS IN SUPERCRITICAL FLID

First equilibrium condition is equality of the solute
fugacity in both solid and supercritical fluid phases:
$\hat{\mathbf{f}}_{i}^{\text {solid }}=\hat{\mathbf{f}}_{i}^{\text {sup ercriticalfluid }}$
Solubility of supercritical fluid in solid phase is negligible;therefore, solid phase is supposed as a pure solid. By assuming that the solid phase is incompressible, and that the molar volume of the solid is constant, the following correlation is obtained:
$\hat{\mathbf{f}}_{i}^{\text {solid }}=\mathbf{P}_{i}^{\text {sat }} \hat{\phi}_{i}^{\text {sat.s }} \exp \left[\frac{\mathbf{v}_{i}^{s}\left(\mathbf{P}-\mathbf{P}_{i}^{\text {sat }}\right)}{\mathbf{R T}}\right]$
where P is pressure, $P_{i}^{\text {sat }}$ is sublimation pressure, $\widehat{\emptyset}_{i}^{\text {sat.s }}$ is the fugacity coefficient of solute $i$ at saturation, $R$ is the universal constant, T is temperature and $v_{i}^{s}$ is solid molar volume.

Fugacity of solute " $i$ " in the supercritical fluid phase is obtained from the following equation:
$\hat{\mathbf{f}}_{\mathbf{i}}^{\text {supercritical }}=\mathbf{y}_{\mathbf{i}} \hat{\phi}_{\mathbf{i}} \mathbf{P}$
where $\widehat{\emptyset}_{i}$ is the fugacity coefficient of solute $i$ in the supercritical fluid solvent.

Following relationship is used to calculate mole fraction of solid:
$y_{2}=\frac{P^{\text {sat }}}{P} \frac{\hat{\phi}_{2}^{\text {sat }}}{\hat{\phi}_{2}} \exp \left[\frac{v_{2}^{s}\left(P-P_{2}^{\text {sat }}\right)}{R T}\right]$
where subscript 2 indicates the heavy solute component.

The sublimation pressure is obtained from the Antoine equation:
$\log \mathbf{P}^{\text {sat }}=\mathbf{A}^{\prime}-\frac{\mathbf{B}^{\prime}}{\mathbf{T}(\mathbf{K})-\mathbf{C}^{\prime}}$
where ${ }_{\bar{A} . \bar{B}, \bar{C}}$ are constant.
The fugacity coefficient of solute in the supercritical fluid solvent is determined by using a cubic equation of state (EOS). The general form of a cubic EOS is given by:
$\mathbf{P}=\frac{\mathbf{R T}}{\mathbf{v}-\mathbf{b}}-\frac{\mathbf{a}}{\mathbf{v}^{2}+\mathbf{U v}+\mathbf{W}}$
Depending on numerical values of U and W , various equations of state can be obtained.

For the case of $\mathrm{U}=\mathrm{b}$ and $\mathrm{W}=0$, the Soave-RedlichKwong (SRK)EOS with the following two parameters is derived:
$\mathrm{a}=0.42747 \mathrm{R}^{2} \mathrm{~T}_{\mathrm{C}}^{2} \alpha\left(\mathrm{~T}_{\mathrm{r}}\right) / \mathrm{P}_{\mathrm{C}}$

## Full Papor

$\mathrm{b}=0.08664 \mathrm{RT} \mathrm{C}_{\mathrm{C}} / \mathbf{P}_{\mathrm{C}}$
where
$\alpha\left(T_{r}\right)=\left(1+m\left(1-T_{r}^{0.5}\right)\right)^{2}$
$\mathrm{m}=0.480+1.574 \omega-0.176 \omega^{2}$
$\omega$ is acentric factor.
Incorporation of $U=2 b, W=b^{2}$ in Eq. (6) leads to the Peng-Robinson (PR) EOS with the following parameters:
$\mathrm{a}=0.45724 \mathrm{R}^{2} \mathrm{~T}_{\mathrm{C}}^{2} \alpha\left(\mathrm{~T}_{\mathrm{r}}\right) / \mathrm{P}_{\mathrm{C}}$
$\mathrm{b}=0.07778 R T_{\mathrm{C}} / \mathbf{P}_{\mathrm{C}}$
where
$\mathrm{m}=0.37464+1.54226 \omega-0.26992 \omega^{2}$
PR and SRK equations of state with four mixing rules (VdW1, VdW2, CVD, and new mixing rules) have been applied to estimate solid solubility in supercritical carbon dioxide. The mixing rules are summarized in TABLE 1.

TABLE 1: Summary of the mixing rules used in this work.

| Mixing rules | Functional form | Refs. |
| :--- | :---: | :---: |
| VdW1 $a=\sum \sum x_{i} x_{j} \sqrt{a_{i} a_{j}}\left(1-k_{i j}\right), b=\sum x_{i} b_{i}$ | [14] |  |
| $a=\sum \sum x_{i} x_{j} \sqrt{a_{i} a_{j}}\left(1-k_{i j}\right)$ |  |  |

VdW2

$$
\begin{equation*}
b=\sum \sum x_{x} x_{f}\left(\frac{b_{+}+b_{j}}{2}\right)\left(1-l_{v}\right) \tag{14}
\end{equation*}
$$

CVD

$$
\begin{equation*}
a=\sum \sum x_{i} x_{j} a_{i j}\left(\frac{b}{b_{i}}\right)^{m_{i}}, b=\sum x_{i} b_{i} \tag{15}
\end{equation*}
$$

$$
a=\sqrt{\left(a_{i} a_{j}\right)} \quad b=\sqrt{\left(b_{i} b_{j}\right)}
$$

In this study, a new mixing rule has been developed based on the Lenard-Jones parameters that obtained from Kirkwood-Müller formula. At first solid surface is assumed as a plate contacted with carbon dioxide molecules then interaction energy between $\mathrm{CO}_{2}$ can be calculated by Lenard-Jones 6-12 potential ${ }^{[10,11]}$ :
$\varepsilon_{12}(\mathrm{z})=4 \varepsilon_{12}^{*}\left[\left(\frac{\sigma}{\mathrm{z}}\right)^{12}-\left(\frac{\sigma}{\mathrm{z}}\right)^{6}\right]$
The interaction of one molecule $\mathrm{CO}_{2}$ and an infinite layer plane of solid molecules is obtained ${ }^{[10-12]}$ :

where is the number of solid molecules/surface unit, is dispersion constant which is calculated by KirkwoodMüller formula as follows:

$$
\begin{equation*}
\mathrm{A}_{\mathrm{s}}=\frac{6 \mathrm{~m}^{\prime} \mathrm{c}^{2} \alpha_{\mathrm{s}} \alpha_{\mathrm{A}}}{\frac{\alpha_{\mathrm{s}}}{\chi_{\mathrm{s}}}+\frac{\alpha_{\mathrm{A}}}{\chi_{\mathrm{A}}}} \tag{16}
\end{equation*}
$$

where $\dot{m}$ is the mass of one electron, c is the speed of light, $\chi_{\mathrm{A}}$ and $\chi_{\mathrm{S}}$ are polarizabilities of $\mathrm{CO}_{2}$ and solid respectively, and $\boldsymbol{\alpha}_{\mathrm{A}}$ and $\boldsymbol{\alpha}_{\mathrm{s}}$ are magnetic susceptibilities of $\mathrm{CO}_{2}$ and solid respectively.
$\sigma$ is the intermolecular distance at zero-interaction energy $\sigma=(2 / 5)^{(1 / 6)} d_{0}=0.858 d$ and $d_{0}$ is the average of $\mathrm{CO}_{2}$ and solid molecule diameters. is the intermolecular distance between $\mathrm{CO}_{2}$ and solid molecule. In this study, we suppose that the solid surface $z$ is covered by $\mathrm{CO}_{2}$; As a result z is summation of radius of solid and $\mathrm{CO}_{2}$; then we have:
$\frac{\sigma}{\mathrm{z}}=\frac{0.858 \times \mathrm{d}_{0}}{\frac{1}{2}\left(\mathrm{~d}_{1}+\mathrm{d}_{2}\right)}=\frac{0.858 \times \frac{1}{2}\left(\mathrm{~d}_{1}+\mathrm{d}_{2}\right)}{\frac{1}{2}\left(\mathrm{~d}_{1}+\mathrm{d}_{2}\right)}=0.858$
where $\mathrm{d}_{1}$ and $\mathrm{d}_{2}$ are $\mathrm{CO}_{2}$ and solid molecule diameters. and:
$\boldsymbol{\varepsilon}(\mathrm{z})=\frac{\mathrm{N}_{\mathrm{s}} \mathrm{A}_{\mathrm{s}}}{2 \sigma^{4}}\left[\mathbf{0 . 8 5 8}{ }^{10}-\mathbf{0 . 8 5 8} \mathbf{8}^{4}\right]=-\mathbf{0 . 1 6 2 8 6 4} \frac{\mathrm{N}_{\mathrm{s}} \mathrm{A}_{\mathrm{s}}}{\sigma^{4}}$
polarizability can be predicted by the following correlation ${ }^{[13]}$ :
$\alpha=\left(\frac{3}{4 \pi N_{\mathrm{A}}}\right) \times\left(\frac{\mathrm{M}}{\rho}\right) \times\left(\frac{\mathrm{n}^{2}-1}{\mathrm{n}^{2}+2}\right)$
where $\mathrm{N}_{\mathrm{A}}$ is Avogadro's number, $M$ is molecular weight, $\rho$ is absolute density and $n$ is refractive index.

## Calculation of second virial coefficient

We have following equations for second virial coefficient:
$B=\lim _{\rho \rightarrow 0} \frac{\partial Z}{\partial \rho}$
$\frac{\partial \mathbf{Z}}{\partial \rho}=\frac{\mathbf{b}}{(\mathbf{1}-\mathbf{b} \rho)^{2}}-\frac{\mathbf{a}}{\mathbf{R T}}\left[\frac{\mathbf{1}-\mathbf{c}_{1} \mathbf{c}_{2} \mathbf{b}^{2} \rho^{2}}{\left(\mathbf{c}_{1} \mathbf{c}_{2} \mathbf{b}^{2} \rho^{2}+\left(\mathbf{c}_{1}+\mathbf{c}_{2}\right) \mathbf{b} \rho+\mathbf{1}\right)^{2}}\right]$
$B=b-\frac{a}{R T}$
$B_{i j}=2 \pi N_{A} \int_{0}^{\infty}\left[1-e^{-\Gamma_{i j}(r) / k T}\right] r^{2} d r$
$\left(b-\frac{a}{R T}\right)_{i j}=2 \pi N_{A} \int_{0}^{\infty}\left[1-e^{-\Gamma_{i j}(r) / k T}\right] r^{2} d r$
The integral equation that is mentioned above is replaced by two function in which one of them is in terms of $\mathrm{a}_{\mathrm{ij}}$ and another one is in terms of $\mathrm{b}_{\mathrm{ij}}$.
$2 \pi N_{A} \int_{0}^{*}\left[1-e^{-\Gamma_{t}(t) k \pi}\right] r^{2} d r \approx H\left(\varepsilon / \omega P_{c}, T^{*} / \sigma^{3}\right)-F\left(\varepsilon / \omega P_{C}, T^{*} / \sigma\right)(\mathbf{2 5})$
where $H$ and $F$ are equivalent to $\mathrm{b}_{\mathrm{ij}}$ and $\mathrm{a}_{\mathrm{ij}}$, respectively.

$$
\begin{align*}
& \mathbf{H}=\mathbf{p}\left(\frac{\mathbf{g}_{0} \varepsilon_{12}}{\omega \mathbf{P}_{\mathrm{C}}}\right)^{\mathrm{q}}\left(\frac{\mathrm{~T}^{*}}{\sigma^{3}}\right)^{\mathrm{r}}-\mathbf{L}^{\prime}  \tag{26}\\
& \mathbf{F}=\mathbf{p}\left(\frac{\mathbf{g}_{0} \varepsilon_{12}}{\omega \mathbf{P}_{\mathrm{c}}}\right)^{\mathrm{q}}\left(\frac{\mathbf{T}^{*}}{\sigma}\right)^{\mathrm{r}}-\mathbf{K}^{\prime} \text { and } \mathbf{g}_{0}=10^{22}  \tag{27}\\
& T^{*}=\frac{T}{T_{C}} \tag{28}
\end{align*}
$$

where $\mathrm{P}_{\mathrm{C}}$ and $\mathrm{T}_{\mathrm{C}}$ are critical pressure and temperature, Tis temperature, $\omega$ is acentric factor, $\varepsilon_{12}$ is interaction energy between solid and $\mathrm{CO}_{2}$, and p, q, r, $\dot{K}^{\prime}$ and $\hat{L}$ are constant. After optimization with experimental and theoretical values, constant parameters are obtained and $\mathrm{p}, \mathrm{q}$ and r are shown in TABLE 2. These values are in general condition when there is no experimental data. It is better to optimize the parameters with experimental data for each solid using the values in TABLE 2 as an initial guess.
TABLE 2 : Constant of H and F function for PR and SRK EOS's.

|  | $\mathbf{H}(\mathbf{P R})$ | $\mathbf{H}(\mathbf{S R K})$ | F(PR \& SRK) |
| :---: | :---: | :---: | :---: |
| p | 0.0082 | 0.0168 | 21.5288 |
| q | -0.5697 | -0.5822 | -0.4951 |
| r | -0.5813 | -0.4557 | -0.1255 |

In order to simplify the mixing rule, an optimization program was coded to find an alternative mixing rule in terms of equation of state parameters, as a result, the following mixing rules was obtained with the same result compared to above $\mathrm{b}_{\mathrm{ij}}$ and $\mathrm{a}_{\mathrm{ij}}$ in the calculations:
$a_{m}=\Sigma \sum x_{i} x_{j} \sqrt{a_{i} a_{j}} Q\left(\frac{b_{i}+b_{j}}{2}\right)^{m_{i j}}\left(1-k_{i j}\right)$
if $\left\{\begin{array}{l}i \neq j \rightarrow m_{i j}=0 \\ i \neq \operatorname{CO}_{2} \rightarrow m_{i j}=0 \\ i=j \rightarrow k_{i j}=0\end{array}\right.$
$b_{m}=\sum \sum \mathbf{x}_{i} \mathbf{x}_{\mathrm{j}}\left(\frac{\mathbf{b}_{\mathrm{i}}+b_{j}}{2}\right)\left(1-\mathrm{l}_{\mathrm{ij}}\right)$
if : $i=j \rightarrow l_{i j}=0$
where $\mathrm{k}_{\mathrm{ij}}, 1_{\mathrm{ij}}$ and $\mathrm{m}_{\mathrm{ij}}$ are interaction coefficients between components of $i$ and $j$ and $Q$ is a fitting parameter that is highly close to one.

In this work, 18 different hydrocarbon solids are studied. Experimental data of solid solubility in supercritical carbon dioxide at different pressure and temperature are applied to calculate and to compare between various mixing rules with PR and SRK EOS's.

The adjustable parameters of each mixing rule are optimized by simplex method and the Absolute Average Relative Deviation is defined as follows:
$A A R D=\sum_{i}^{N}\left(\left|\frac{y_{\text {solid }, i}^{\exp }-y_{\text {solid }, i}}{y_{\text {solid }, i}^{\operatorname{ecp} .}}\right| \frac{1}{n}\right) \cdot 100$
where N is number of solubility data point, $y_{\text {solidi }, i}^{\text {exp. }}$ is $i$ h experimental data point of solid solubility and $y_{\text {solid }, i}^{\text {calc }}$ is ith calculated data point of solid solubility

## RESULTS AND DISCUSSION

The critical constants, acentric factors and solid molar volumes of 18 compounds are listed in TABLE 3. TABLE 4 shows the constants of Antoine equation. Different combinations of the PR and the SRK EOS's with four mixing rules are mentioned in this study to calculate the solubilities of solid compounds in supercritical carbon dioxide. TABLE 5 shows the comparison of our calculated results with two EOS's and four mixing rules based on Average Absolute Relative Deviation Percent (AARD (\%)) and the optimized interaction coefficients between components of $i$ and $j\left(k_{i j}, 1_{i j}, m_{i j}\right)$ are presented too. TABLE 5 shows that AARD (\%) for the new mixing rule in the same equations of state, is minimum in compare with the other mixing rules that are discussed here.

Figure 1 and Figure 2 show the comparison of our calculated results with the experimental data for 1Hexadecanol, 1-Octadecanol, Stearic acid and Palm-

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itic acid in supercritical carbon dioxide by using PR EOS at 338 K and SRK EOS at 328 K , respectively. Figure 3 shows the comparison of our calculated results with
the experimental data for 2,5-Xylenol, Benzoin, 3-4Xylenol, Fluorene, Mandelic Acid, Naphthalene, Pyrene and Propyl-4-hydroxy benzoate in supercritical carbon

TABLE 3: Physical properties of the studied components

| Component | $T_{C}(\mathbf{K})$ | $P_{C}$ (bar) | $\omega$ | Refs. | $v_{2}^{5}(\mathbf{l} / \mathrm{mol})$ | Refs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Carbon dioxide (solvent) | 304.2 | 73.7 | 0.225 | [16] | - | - |
| Benzoin | 853.52 | 26.6 | 0.599 | [17,18,19] | 0.162 | [20] |
| Anthracene | 869.15 | 30.8 | 0.353 | [15] | 0.1426 | [15,17,21-23] |
| Pyrene | 936 | 25.7 | 0.509 | [24] | 0.1585 | [17] |
| Mandelic Acid | 903.79 | 34.73 | 0.645 | [17,18,19] | 0.117 | [25] |
| Propyl-4-hydroxy benzoate | 815.92 | 31.3 | 0.722 | [17,18,19] | 0.1316 | [26] |
| 3-4-Xylenol | 729.8 | 49 | 0.576 | [16,27] | 0.1243 | [27] |
| 2,5-Xylenol | 706.9 | 48 | 0.569 | [16,27] | 0.1257 | [27,28] |
| Naphthalene | 748.4 | 40.51 | 0.302 | [29,30] | 0.111 | [31] |
| Phenanthrene | 882.65 | 31.715 | 0.437 | [32] | 0.182 | [31] |
| Fluorene | 826.4 | 29.5 | 0.406 | [15] | 0.1393 | [17,33] |
| 2,6-Dimethyl naphthalene | 777 | 31.8 | 0.42 | [34] | 0.1392 | [17] |
| 2,7-Dimethyl naphthalene | 777 | 32.2 | 0.42 | [31,35] | 0.136 | [35,36] |
| O-hydroxy benzoic acid | 739 | 51.8 | 0.832 | [37] | 0.0957 | [38] |
| P-hydroxy benzoic acid | 739 | 51.8 | 0.832 | [37] | 0.0924 | [38] |
| 1-Hexadecanol | 761 | 14.9 | 0.748 | [4] | 0.2965 | [39] |
| 1-Octadecanol | 777 | 13.4 | 0.863 | [4] | 0.333 | [39] |
| Palmitic acid | 776 | 14.9 | 1.083 | [4] | 0.2857 | [40] |
| Stearic acid | 779 | 13.4 | 1.084 | [4] | 0.3024 | [39,41] |

TABLE 4 : Constant of Antoine equation

| Component | $A$ | $\dot{B}$ | $\dot{C}$ | Pressure unit | Refs. |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Naphthalene | 8.583 | 3733.9 | 0 | bar | $[42]$ |
| Phenanthrene | 9.631 | 4873.4 | 0 | bar | $[43]$ |
| Anthracene | 9.775 | 5313.7 | 0 | bar | $[29]$ |
| Fluorene | 9.429 | 4419.5 | 0 | bar | $[25]$ |
| Pyrene | 8.3496 | 4904 | 0 | bar | $[29]$ |
| 2,6-Dimethyl naphthalene | 9.429 | 4419.5 | 0 | bar | $[29]$ |
| 2,7-Dimethyl naphthalene | 12.431 | 4388.11 | 0 | mmHg | $[35]$ |
| 1-Hexadecanol | 22.773 | 8736 | 0 | kPa | $[44]$ |
| 1-Octadecanol | 24.99 | 9787 | 0 | kPa | $[44]$ |
| Palmitic acid | 19.342 | 8069 | 0 | kPa | $[44]$ |
| Stearic acid | 6.171 | 2157.5 | 153.78 | kPa | $[44]$ |
| 2,5-Xylenol | 15.495 | 4438.6 | 0 | Pa | $[45]$ |
| 3-4-Xylenol | 15.298 | 4478.2 | 0 | Pa | $[45]$ |
| Mandelic acid | $49.83^{\mathrm{a}}$ | $17256.62^{\mathrm{a}}$ | $0^{\mathrm{a}}$ | Pa | $[46]$ |
| Benzoin | $36.38^{\mathrm{a}}$ | $13160.97^{\mathrm{a}}$ | $0^{\mathrm{a}}$ | Pa | $[46]$ |
| Propyl-4-hydroxy benzoate | $41.15^{\mathrm{a}}$ | $14209.69^{\mathrm{a}}$ | $0^{\mathrm{a}}$ | Pa | $[46]$ |
| O-hydroxy benzoic acid | $2.25 \mathrm{E}-6 @ 45^{\circ} \mathrm{C}^{\mathrm{b}}$ |  |  | bar | $[37]$ |
| P-hydroxy benzoic acid | $6.65 \mathrm{E}-6 @ 55^{\circ} \mathrm{C}^{\mathrm{b}}$ |  |  | bar | $[37]$ |
|  | $1.37 \mathrm{E}-8 @ 45^{\circ} \mathrm{C}^{\mathrm{b}}$ |  |  |  |  |

${ }^{\mathrm{a}} \ln \mathrm{P}^{\text {sat }}=\mathrm{A}-\frac{\mathrm{B}}{\mathrm{T}(\mathrm{K})-\mathrm{C}} ;{ }^{\mathrm{b}}$ Sublimation pressure

TABLE 5: Optimized interaction coefficients between components of $i$ and $j$ and average absolute relative deviation percent for the solubility of pure component in supercritical $\mathrm{CO}_{2}$ with four different mixing rules using the PR and SRK EOS's.

| Component | T(K) | P(bar) | $\mathbf{N a}^{\text {a }}$ | EOS | AARD (\%) |  |  |  | $k_{i j}$ | $l_{i j}$ | $m_{i j}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | VdW1 | VdW2 | CVD | This Work |  |  |  |
| Benzoin [46] | 308.15 | 121.6-236.1 | 6 | PR | 2.8292 | 2.6338 | 2.673 | 2.4928 | 0.0906 | 0.0090 | -0.0012 |
|  |  |  |  | SRK | 3.7486 | 2.6898 | 4.6249 | 2.5954 | 0.1008 | 0.0385 | -0.0023 |
|  | 318.15 | 111.3-244.3 | 7 | PR | 3.9081 | 4.3922 | 3.5001 | 3.0957 | 0.0911 | 0.0402 | -0.0001 |
|  |  |  |  | SRK | 5.2831 | 3.3924 | 5.0384 | 3.4223 | 0.0987 | 0.0385 | -0.0008 |
| Anthracene [47] | 328.15 | 114.8-244.3 | 6 | PR | 10.2256 | 4.366 | 10.2674 | 1.1958 | 0.0901 | 0.0215 | 0.0043 |
|  |  |  |  | SRK | 10.8436 | 5.949 | 8.6901 | 2.4733 | 0.0973 | 0.0210 | 0.0043 |
|  | 318.15 | 84.4-564.4 | 4 | PR | 28.4037 | 24.7712 | 27.8199 | 6.3541 | $2.10 \mathrm{E}-16$ | 0.1850 | -0.0250 |
|  |  |  |  | SRK | 28.8286 | 24.6342 | 28.2802 | 4.1721 | 0.0300 | 0.2450 | -0.0300 |
|  | 323.15 | 89-836.3 | 6 | PR | 24.3418 | 25.5412 | 24.5633 | 7.2509 | 0.0500 | 0.2850 | -0.0350 |
|  |  |  |  | SRK | 31.3374 | 27.1708 | 33.4898 | 6.5453 | 0.0800 | 0.3450 | -0.0400 |
|  | 328.15 | 94.7-89.09 | 5 | PR | 27.5037 | 22.7695 | 29.1631 | 4.0347 | 0.0450 | 0.2850 | -0.0400 |
|  |  |  |  | SRK | 35.6341 | 24.0610 | 37.7778 | 5.5060 | 0.0650 | 0.3300 | -0.0450 |
|  | 358.15 | 129-930.3 | 6 | PR | 18.1184 | 17.1583 | 18.2654 | 14.4283 | 0.0100 | 0.2350 | -0.0300 |
|  |  |  |  | SRK | 25.7956 | 18.6818 | 24.1200 | 14.3251 | 0.0350 | 0.3000 | -0.0400 |
|  | 363.15 | 132.6-975.7 | 6 | PR | 16.9620 | 16.4691 | 16.7251 | 13.5154 | 0.0050 | 0.2300 | -0.0300 |
|  |  |  |  | SRK | 26.4216 | 17.8756 | 24.829 | 13.9934 | 0.0300 | 0.3000 | -0.0450 |
| Pyrene [19,48] | 368.15 | 137-1020.5 | 5 | PR | 21.3167 | 20.1808 | 21.4619 | 14.8580 | 0.0150 | 0.2700 | -0.0550 |
|  |  |  |  | SRK | 28.2421 | 22.4729 | 27.8522 | 14.8614 | 0.0350 | 0.3300 | -0.0700 |
|  |  |  |  | PR | 30.6695 | 13.7620 | 30.9967 | 7.3232 | 0.2600 | 0.3600 | -0.0100 |
|  | 308.15 | 83.6-483.4 | 7 | SRK | 37.5088 | 16.0310 | 35.8357 | 7.9719 | 0.2850 | 0.4050 | -0.0150 |
|  |  |  |  | PR | 11.6926 | 11.4037 | 12.1831 | 5.4511 | 0.2050 | 0.2350 | -0.0050 |
|  |  | $80.4-203.5$ | , | SRK | 13.2584 | 12.5155 | 13.6199 | 6.4711 | 0.2200 | 0.2500 | -0.0050 |
| Pyrene [19,48] | 318.2 | 95-254 | 20 | PR | 9.4866 | 8.7079 | 9.4178 | 3.6209 | 0.2300 | 0.3000 | -0.0100 |
|  |  |  |  | SRK | 11.2353 | 10.1302 | 11.2394 | 4.8605 | 0.2600 | 0.3550 | -0.0150 |
|  | 323.15 | 104.3-483.4 | 7 | PR | 36.0100 | 7.4995 | 34.1467 | 8.0844 | 0.2450 | 0.3400 | -0.0100 |
|  |  |  |  | SRK | 38.2325 | 10.7713 | 41.7837 | 6.6957 | 0.2600 | 0.3650 | -0.0100 |
|  |  |  |  | PR | 5.1136 | 4.7663 | 4.4540 | 3.2411 | 0.1850 | 0.2000 | -0.0050 |
|  | 323.2 | 100.1-228.5 | 35 | SRK | 6.0415 | 6.9306 | 5.4578 | 3.2414 | 0.2200 | 0.2650 | -0.0100 |
| Mandelic Acid [46] | 328.2 | 105.245 | 20 | PR | 6.7645 | 6.1578 | 5.8100 | 3.4319 | 0.2300 | 0.3050 | -0.0150 |
|  |  |  |  | SRK | 7.1908 | 7.5917 | 6.9991 | 2.6587 | 0.2350 | 0.3050 | -0.0150 |
|  | 343.15 | 104.3-483.4 | 8 | PR | 55.5147 | 24.7147 | 53.3595 | 21.5114 | 0.2300 | 0.3250 | -0.0150 |
|  |  |  |  | SRK | 52.5814 | 22.1344 | 53.1025 | 17.3982 | 0.2550 | 0.3750 | -0.0200 |
|  |  |  |  | PR | 37.0743 | 6.2913 | 37.4339 | 7.8740 | 0.2000 | 0.4700 | 0.0050 |
|  | 308.15 | 101-228.5 | 7 | SRK | 37.2863 | 6.652 | 39.6686 | 7.4203 | 0.2200 | 0.5150 | 0.0050 |
|  |  |  |  | PR | 31.6307 | 5.1715 | 33.2679 | 2.6531 | 0.2750 | 0.6500 | -0.0050 |
|  | 318.15 | 102.3-225.7 | 7 | SRK | 36.1244 | 5.1098 | 36.4133 | 2.7383 | 0.2850 | 0.6800 | -0.0050 |
|  |  |  |  | PR | 31.5318 | 10.3430 | 30.3295 | 9.1046 | 0.2800 | 0.6800 | -0.0050 |
|  | 328.15 | 104.4-230.6 | 7 | SRK | 29.0384 | 10.8282 | 30.4613 | 9.8902 | 0.2850 | 0.7000 | -0.0050 |
| Propyl-4-hydroxy benzoate [46] | 308.15 | 94.1-220.9 | 7 | PR | 13.5994 | 2.1176 | 14.3637 | 1.5054 | 0.2350 | 0.4200 | -0.0050 |
|  |  |  |  | SRK | 15.6949 | 2.6009 | 17.2696 | 1.1920 | 0.2400 | 0.4200 | -0.0050 |


| Component | T(K) | $\mathbf{P}$ (bar) | $\mathbf{N}^{\mathbf{a}}$ | EOS | AARD(\%) |  |  |  | $k_{i j}$ | $l_{i j}$ | $m_{i j}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | VdW1 | VdW2 | CVD | This Work |  |  |  |
| Benzoin [46] | 308.15 | 121.6-236.1 | 6 | PR | 2.8292 | 2.6338 | 2.673 | 2.4928 | 0.0906 | 0.0090 | -0.0012 |
|  |  |  |  | SRK | 3.7486 | 2.6898 | 4.6249 | 2.5954 | 0.1008 | 0.0385 | -0.0023 |
|  | 318.15 | 111.3-244.3 | 7 | PR | 3.9081 | 4.3922 | 3.5001 | 3.0957 | 0.0911 | 0.0402 | -0.0001 |
|  |  |  |  | SRK | 5.2831 | 3.3924 | 5.0384 | 3.4223 | 0.0987 | 0.0385 | -0.0008 |
|  | 328.15 | 114.8-244.3 | 6 | PR | 10.2256 | 4.366 | 10.2674 | 1.1958 | 0.0901 | 0.0215 | 0.0043 |
|  |  |  |  | SRK | 10.8436 | 5.949 | 8.6901 | 2.4733 | 0.0973 | 0.0210 | 0.0043 |
| Anthracene [47] | 318.15 | 84.4-564.4 | 4 | PR | 28.4037 | 24.7712 | 27.8199 | 6.3541 | $2.10 \mathrm{E}-16$ | 0.1850 | -0.0250 |
|  |  |  |  | SRK | 28.8286 | 24.6342 | 28.2802 | 4.1721 | 0.0300 | 0.2450 | -0.0300 |
|  | 323.15 | 89-836.3 | 6 | PR | 24.3418 | 25.5412 | 24.5633 | 7.2509 | 0.0500 | 0.2850 | -0.0350 |
|  |  |  |  | SRK | 31.3374 | 27.1708 | 33.4898 | 6.5453 | 0.0800 | 0.3450 | -0.0400 |
|  | 328.15 | 94.7-89.09 | 5 | PR | 27.5037 | 22.7695 | 29.1631 | 4.0347 | 0.0450 | 0.2850 | -0.0400 |
|  |  |  |  | SRK | 35.6341 | 24.0610 | 37.7778 | 5.5060 | 0.0650 | 0.3300 | -0.0450 |
|  | 358.15 | 129-930.3 | 6 | PR | 18.1184 | 17.1583 | 18.2654 | 14.4283 | 0.0100 | 0.2350 | -0.0300 |
|  |  |  |  | SRK | 25.7956 | 18.6818 | 24.1200 | 14.3251 | 0.0350 | 0.3000 | -0.0400 |
|  | 363.15 | 132.6-975.7 | 6 | PR | 16.9620 | 16.4691 | 16.7251 | 13.5154 | 0.0050 | 0.2300 | -0.0300 |
|  |  |  |  | SRK | 26.4216 | 17.8756 | 24.829 | 13.9934 | 0.0300 | 0.3000 | -0.0450 |
|  |  | 137-1020.5 | 5 | PR | 21.3167 | 20.1808 | 21.4619 | 14.8580 | 0.0150 | 0.2700 | -0.0550 |
|  | 368.15 | 137-1 | 5 | SRK | 28.2421 | 22.4729 | 27.8522 | 14.8614 | 0.0350 | 0.3300 | -0.0700 |
| Pyrene [19,48] | 308.15 | 83.6-483.4 | 7 | PR | 30.6695 | 13.7620 | 30.9967 | 7.3232 | 0.2600 | 0.3600 | -0.0100 |
|  |  |  |  | SRK | 37.5088 | 16.0310 | 35.8357 | 7.9719 | 0.2850 | 0.4050 | -0.0150 |
|  | 308.2 | 80.4-203.5 | 45 | PR | 11.6926 | 11.4037 | 12.1831 | 5.4511 | 0.2050 | 0.2350 | -0.0050 |
|  |  |  |  | SRK | 13.2584 | 12.5155 | 13.6199 | 6.4711 | 0.2200 | 0.2500 | -0.0050 |
|  |  |  |  | PR | 9.4866 | 8.7079 | 9.4178 | 3.6209 | 0.2300 | 0.3000 | -0.0100 |
|  | 318.2 | 95-254 | 20 | SRK | 11.2353 | 10.1302 | 11.2394 | 4.8605 | 0.2600 | 0.3550 | -0.0150 |
| Pyrene [19,48] | 323.15 | 104.3-483.4 | 7 | PR | 36.0100 | 7.4995 | 34.1467 | 8.0844 | 0.2450 | 0.3400 | -0.0100 |
|  |  |  |  | SRK | 38.2325 | 10.7713 | 41.7837 | 6.6957 | 0.2600 | 0.3650 | -0.0100 |
|  | 323.2 | 100.1-228.5 | 35 | PR | 5.1136 | 4.7663 | 4.4540 | 3.2411 | 0.1850 | 0.2000 | -0.0050 |
|  |  |  |  | SRK | 6.0415 | 6.9306 | 5.4578 | 3.2414 | 0.2200 | 0.2650 | -0.0100 |
|  | 328.2 | 105.245 | 20 | PR | 6.7645 | 6.1578 | 5.8100 | 3.4319 | 0.2300 | 0.3050 | -0.0150 |
|  |  |  |  | SRK | 7.1908 | 7.5917 | 6.9991 | 2.6587 | 0.2350 | 0.3050 | -0.0150 |
|  | . 15 | 104.3-483.4 | 8 | PR | 55.5147 | 24.7147 | 53.3595 | 21.5114 | 0.2300 | 0.3250 | -0.0150 |
|  | .15 | 104.3-483.4 | 8 | SRK | 52.5814 | 22.1344 | 53.1025 | 17.3982 | 0.2550 | 0.3750 | -0.0200 |
| Mandelic Acid [46] | 308.15 | 101-228.5 | 7 | PR | 37.0743 | 6.2913 | 37.4339 | 7.8740 | 0.2000 | 0.4700 | 0.0050 |
|  |  |  |  | SRK | 37.2863 | 6.652 | 39.6686 | 7.4203 | 0.2200 | 0.5150 | 0.0050 |
|  | 318.15 | 102 3-225.7 | 7 | PR | 31.6307 | 5.1715 | 33.2679 | 2.6531 | 0.2750 | 0.6500 | -0.0050 |
|  | 318.15 | 102.3-225.7 | 7 | SRK | 36.1244 | 5.1098 | 36.4133 | 2.7383 | 0.2850 | 0.6800 | -0.0050 |
|  | 328.15 | 104.4-230.6 | 7 | PR | 31.5318 | 10.3430 | 30.3295 | 9.1046 | 0.2800 | 0.6800 | -0.0050 |
|  | 328.15 | 104.4-230.6 | 7 | SRK | 29.0384 | 10.8282 | 30.4613 | 9.8902 | 0.2850 | 0.7000 | -0.0050 |
| Propyl-4-hydroxy benzoate [46] | 308.15 | 94.1-220.9 | 7 | PR | 13.5994 | 2.1176 | 14.3637 | 1.5054 | 0.2350 | 0.4200 | -0.0050 |
|  |  |  |  | SRK | 15.6949 | 2.6009 | 17.2696 | 1.1920 | 0.2400 | 0.4200 | -0.0050 |
|  | 318.15 | 96.8-214.7 | 7 | PR | 14.2196 | 8.1911 | 14.0412 | 2.7169 | 0.2850 | 0.5400 | -0.0100 |
|  |  |  |  | SRK | 15.4313 | 8.8246 | 15.1762 | 3.0757 | 0.2850 | 0.5350 | -0.0100 |
|  | 328.15 | 105.1-220.2 | 7 | PR | 18.0685 | 17.7706 | 18.0141 | 2.0883 | 0.4800 | 0.9700 | -0.0350 |
|  |  |  |  | SRK | 18.6907 | 18.3623 | 19.0544 | 2.1674 | 0.4800 | 0.9800 | -0.0400 |
| 3-4-Xylenol [27] | 308.15 | 82-262 | 7 | PR | 23.0053 | 8.6598 | 22.7541 | 1.5214 | -0.0600 | -0.1250 | -0.0050 |
|  |  |  |  | SRK | 22.0859 | 9.2925 | 21.601 | 2.2491 | -0.0050 | -8.21E-16 | -0.0100 |
| 2,5-Xylenol [28] | 308.15 | 87-267 | 7 | PR | 26.6876 | 6.0457 | 26.5655 | 1.8053 | -0.0500 | -0.0850 | -0.0100 |
|  |  |  |  | SRK | 25.4857 | 7.1183 | 25.7471 | 1.5935 | -0.0350 | -0.0650 | -0.0100 |


| Component | T(K) | P(bar) | $\mathbf{N}^{\text {a }}$ | EOS | AARD(\%) |  |  |  | $k_{i j}$ | $l_{i j}$ | $m_{i j}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | VdW1 | VdW2 | CVD | This Work |  |  |  |
| Naphthalene [49] | 308.15 | 86.8-255.3 | 9 | PR | 11.2797 | 4.9591 | 11.1225 | 1.4325 | 0.0800 | 0.2000 | -0.0100 |
|  |  |  |  | SRK | 10.7920 | 5.6464 | 9.5160 | 1.6425 | 0.0850 | 0.2050 | -0.0100 |
| Naphthalene [49] | 333.55 | 108.4-291.4 | 19 | PR | 5.9033 | 4.3151 | 5.63 | 3.8172 | -0.1850 | -0.2900 | 0.0400 |
|  |  |  |  | SRK | 6.5240 | 4.1782 | 6.6265 | 4.0712 | -0.0500 | 0.0550 | 0.0200 |
|  | 8.0 | 151.8232 .2 | 7 | PR | 3.7213 | 1.9292 | 3.7518 | 1.0550 | 0.2150 | 0.6350 | -0.0200 |
|  | 338.05 | 151.8-232.2 | 7 | SRK | 5.0398 | 2.1961 | 4.2844 | 0.9533 | 0.1900 | 0.6000 | -0.0200 |
| Phenanthrene [48,50] | 308.2 | 78.3-203.5 | 47 | PR | 19.3415 | 12.3779 | 18.7357 | 4.8184 | 0.1050 | 0.0900 | -0.0050 |
|  |  |  |  | SRK | 18.1881 | 13.1176 | 17.8897 | 5.6411 | 0.1200 | 0.1050 | -0.0050 |
|  | 318.2 | 95-254 | 20 | PR | 17.4822 | 7.7594 | 17.1394 | 4.2555 | 0.1100 | 0.1200 | -0.0100 |
|  |  |  |  | SRK | 15.9964 | 8.9711 | 15.1638 | 3.8964 | 0.1250 | 0.1400 | -0.0100 |
|  | 323.2 | 89.4-228.5 | 38 | PR | 17.7502 | 5.7279 | 18.0258 | 5.1786 | 0.0700 | 0.0250 | -0.0050 |
|  |  |  |  | SRK | 19.2049 | 6.7354 | 17.9363 | 5.4091 | 0.0800 | 0.0300 | -0.0050 |
|  | 328 | 90-245 | 23 | PR | 19.9165 | 4.8743 | 19.3509 | 3.1093 | 0.0850 | 0.0650 | -0.0100 |
|  | 328.2 | 90-245 | 23 | SRK | 19.9606 | 7.7785 | 19.3720 | 3.6395 | 0.1300 | 0.1600 | -0.0150 |
| Fluorene [19,48] | 308.15 | 83.7-414.5 | 6 | PR | 30.0807 | 5.2473 | 28.0864 | 5.2473 | 0.2250 | 0.2800 | $4.34 \mathrm{E}-17$ |
|  |  |  |  | SRK | 33.891 | 6.0112 | 34.2151 | 6.3855 | 0.2500 | 0.3200 | $4.34 \mathrm{E}-17$ |
|  | 308.2 | 78.3-203.5 | 47 | PR | 14.2369 | 9.7064 | 13.1427 | 5.4411 | 0.2650 | 0.3650 | -0.0050 |
|  |  |  |  | SRK | 14.9606 | 10.5292 | 14.1889 | 5.0675 | 0.2650 | 0.3550 | -0.0050 |
|  | 323.15 | 83.7-414.5 | 8 | PR | 42.7946 | 15.2145 | 43.1622 | 15.2145 | 0.2350 | 0.2950 | $4.34 \mathrm{E}-17$ |
|  |  |  |  | SRK | 43.7543 | 11.7959 | 44.4848 | 11.7907 | 0.2550 | 0.3300 | $4.34 \mathrm{E}-17$ |
|  | 323.2 | 83.7-414.5 | 38 | PR | 16.3774 | 8.2093 | 16.9244 | 7.9118 | 0.1950 | 0.1950 | 0.0050 |
|  |  |  |  | SRK | 15.9664 | 6.5014 | 16.5766 | 6.7457 | 0.2050 | 0.2050 | 0.0050 |
|  |  | 85 | 2 | PR | 26.9329 | 11.2076 | 24.5408 | 10.0447 | 0.2650 | 0.3550 | -0.0050 |
|  | 328.2 | 85-245 | 24 | SRK | 21.3068 | 8.4739 | 22.7499 | 7.8974 | 0.2650 | 0.3500 | -0.0050 |
| 2,6-Dimethyl naphthalene [35] | 308.2 | 79-146 | 4 | PR | 33.3766 | 23.4231 | 31.8858 | 5.6955 | -0.0300 | -0.1350 | -0.0050 |
|  |  |  |  | SRK | 31.8981 | 24.1483 | 32.606 | 5.7398 | 0.1300 | 0.2300 | -0.0150 |
|  | 328.2 | 100-127 | 4 | PR | 6.6612 | 2.7170 | 6.2782 | 2.2257 | 0.0300 | 0.0350 | -0.0050 |
|  |  | $100-127$ |  | SRK | 8.6343 | 2.4292 | 9.0369 | 2.8443 | -0.0850 | -0.2900 | 0.0050 |
| 2,7-Dimethyl naphthalene [35] | 308.2 | 88-242 | 5 | PR | 14.8662 | 8.8744 | 14.7062 | 1.0942 | 0.1150 | 0.2000 | -0.0150 |
|  |  |  |  | SRK | 13.6194 | 9.8150 | 13.8143 | 1.0943 | 0.1400 | 0.2450 | -0.0200 |
|  | 328. | 100 | 5 | PR | 16.8066 | 3.3291 | 15.5319 | 1.9836 | 0.0400 | 0.0500 | -0.0050 |
|  |  | $100-24$ |  | SRK | 16.1314 | 5.4781 | 15.8082 | 0.3379 | 0.0750 | 0.1250 | -0.0100 |
| O-hydroxy benzoic acid [51,52] | 318.15 | 81.1-202.6 | 12 | PR | 22.9849 | 5.9596 | 22.9985 | 6.7869 | -0.0500 | -0.0900 | -0.0050 |
|  |  |  |  | SRK | 23.5465 | 6.2956 | 22.7284 | 6.7809 | -0.0400 | -0.0950 | -0.0050 |
|  | 328.15 | 1013-2026 | 11 | PR | 17.6547 | 3.4977 | 17.9277 | 3.3700 | -0.0700 | -0.1050 | -0.0050 |
|  |  | 101.3-202.6 | 11 | SRK | 17.5422 | 4.538 | 17.9908 | 4.1159 | -0.0550 | -0.0850 | -0.0050 |
|  | 328.15 | 101.3202 .6 | 6 | PR | 21.6606 | 1.7615 | 22.2208 | 1.6937 | -0.0850 | -0.1650 | -0.0050 |
|  | 328.15 | 101.3-202.6 |  | SRK | 21.7743 | 2.5635 | 22.3821 | 1.9378 | -0.0700 | -0.1500 | -0.0050 |
| P-hydroxy benzoic acid [52] | 318.15 | 101.3-202.6 | 6 | PR | 19.8779 | 4.8131 | 19.5393 | 1.5374 | -0.0450 | -0.0650 | -0.0050 |
|  |  |  |  | SRK | 19.0202 | 5.2828 | 18.7005 | 1.9857 | -0.0300 | -0.0500 | -0.0050 |
|  | 328.15 | 101.3-202.6 | 6 | PR | 15.8269 | 4.6075 | 14.3667 | 3.9840 | -0.0250 | 0.0450 | -0.0050 |
|  | 328.15 | 101.3-202.6 | 6 | SRK | 15.9321 | 3.4474 | 14.6654 | 2.7469 | -0.0250 | 0.0200 | -0.0050 |
| 1-Hexadecanol [53] | 318 | 152.1-415.1 | 7 | PR | 32.3703 | 2.1009 | 32.3461 | 1.5887 | 0.1300 | 0.2750 | -0.0050 |
|  |  |  |  | SRK | 37.2722 | 3.0008 | 40.4952 | 1.6716 | 0.1700 | 0.3350 | -0.0150 |
|  | 328 | 141.8-415.9 | 5 | PR | 57.0294 | 9.8866 | 52.303 | 8.3203 | 0.1950 | 0.3500 | -0.0050 |
|  |  |  |  | SRK | 58.1061 | 9.9483 | 55.8279 | 7.9504 | 0.2300 | 0.4050 | -0.0150 |
|  | 338 | 147.1-373 | 6 | PR | 48.781 | 4.4550 | 53.802 | 2.4078 | 0.2700 | 0.4350 | -0.0100 |
|  |  |  |  | SRK | 54.967 | 4.7066 | 54.1103 | 2.8447 | 0.3100 | 0.5000 | -0.0250 |

## Full Paper

| Component | T(K) | P(bar) | $\mathbf{N}^{\text {a }}$ | EOS | AARD (\%) |  |  |  | $k_{i j}$ | $t_{i j}$ | $m_{i j}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | VdW1 | VdW2 | CVD | This Work |  |  |  |
| 1-Octadecanol [54] | 318 | 152-437.9 | 4 | PR | 9.5284 | 4.1363 | 9.5890 | 3.0092 | 0.0450 | 0.1250 | -0.0100 |
|  |  |  |  | SRK | 24.0953 | 4.2891 | 23.5500 | 3.3346 | 0.0900 | 0.1750 | -0.0100 |
|  | 328 | 139.9-447.7 | 7 | PR | 56.8142 | 8.4207 | 53.5752 | 4.9818 | 0.1750 | 0.3250 | -0.0150 |
|  |  |  |  | SRK | 58.2835 | 9.2823 | 59.0386 | 5.2869 | 0.2100 | 0.3700 | -0.0200 |
|  |  |  |  | PR | 66.9715 | 3.4795 | 67.0302 | 3.4795 | 0.2150 | 0.3400 | $4.34 \mathrm{E}-17$ |
|  |  |  |  | SRK | 71.4502 | 6.1522 | 66.6701 | 3.2837 | 0.2600 | 0.4100 | -0.0150 |
| Palmitic acid [53] | 318 | 142.1-360.6 | 5 | PR | 30.4772 | 3.7517 | 33.0766 | 2.2303 | 0.1600 | 0.3050 | -0.0100 |
|  |  |  |  | SRK | 42.1376 | 5.1102 | 41.0469 | 1.8748 | 0.2200 | 0.3950 | -0.0300 |
|  | 328 | 144.1-573.5 | 7 | PR | 73.5056 | 5.9974 | 74.4539 | 6.6069 | 0.1500 | 0.2800 | 0.0050 |
|  |  |  |  | SRK | 84.9557 | 6.6040 | 79.5333 | 6.6701 | 0.1950 | 0.3400 | $4.34 \mathrm{E}-17$ |
| Stearic acid [54] | 338 | 142.5-574.8 | 7 | PR | 95.1375 | 14.0898 | 93.5112 | 8.3035 | 0.2450 | 0.4400 | -0.0200 |
|  |  |  |  | SRK | 99.4231 | 15.3601 | 94.1093 | 7.8808 | 0.2800 | 0.4850 | -0.0250 |
|  | 318 | 145.4-361.5 | 6 | PR | 11.0718 | 7.9148 | 10.8864 | 2.7284 | 0.0500 | 0.1500 | -0.0400 |
|  |  |  |  | SRK | 10.2141 | 9.0883 | 8.8103 | 3.2388 | 0.1150 | 0.2450 | -0.0700 |
|  | 328 | 154.8-467.5 | 6 | PR | 57.1116 | 18.3888 | 60.0238 | 4.8699 | 0.0250 | 0.0900 | 0.0350 |
|  |  |  |  | SRK | 71.1858 | 16.6831 | 71.7080 | 7.2859 | 0.0900 | 0.1850 | 0.0250 |
|  | 338 | 161.5-463.8 | 5 | PR | 56.9730 | 11.7971 | 53.8029 | 4.3336 | 0.1950 | 0.4150 | -0.0400 |
|  |  |  |  | SRK | 63.6315 | 13.3366 | 59.1502 | 3.6326 | 0.2250 | 0.4500 | -0.0500 |

a $\mathbf{N}$ is the number of data points


Figure 1 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the PR EOS at $\mathrm{T}=338 \mathrm{~K}$ in the new mixing rule (this work)


Figure 2 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the SRK EOS at $\mathrm{T}=328 \mathrm{~K}$ in the new mixing rule (this work)


[^0]Figure 3 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the PR EOS at $\mathrm{T}=308.15 \mathrm{~K}$ in the new mixing rule (this work).


Figure 4 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the PR EOS at $\mathrm{T}=343.15 \mathrm{~K}$ in the new mixing rule (this work)


Figure 5 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the PR EOS at $\mathrm{T}=318.15 \mathrm{~K}$ in the new mixing rule (this work)


Figure 6 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the PR EOS at $\mathbf{T}=323.15 \mathrm{~K}$ in the new mixing rule (this work).


Figure 7 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the PR EOS at $\mathbf{T}=328.15 \mathrm{~K}$ in the new mixing rule (this work)


Figure 8 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the PR EOS at $\mathrm{T}=328.15 \mathrm{~K}$ in the new mixing rule (this work)


Figure 9 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the SRK EOS at $\mathrm{T}=318 \mathrm{~K}$ in the new mixing rule (this work)


Figure 10 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the SRK EOS at $\mathbf{T}=318.2 \mathrm{~K}$ in the new mixing rule (this work)


Figure 11 : Solubility of solid components in supercritical $\mathrm{C}_{\mathbf{O}}^{2}$ using the SRK EOS at $\mathrm{T}=328.2 \mathrm{~K}$ in the new mixing rule (this work)


Figure 12 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the SRK EOS at $\mathrm{T}=308.2 \mathrm{~K}$ in the new mixing rule (this work)

## Pu00 Papor



Figure 13 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the SRK EOS at $\mathbf{T}=323.2 \mathrm{~K}$ in the new mixing rule (this work)



Figure 14 : Solubility of solid components in supercritical $\mathrm{CO}_{2}$ using the SRK EOS at $\mathrm{T}=318.15 \mathrm{~K}$ in the new mixing rule (this work)
dioxide by using PR EOS at 308.15 K . In this way, Figures 4-14 demonstrate our calculated results with the experimental data for different solids in supercritical carbon dioxide at various temperature and pressure conditions. In all systems, our predicted results are in close agreement to the experimental data.

## NOMENCLATURE

| a | energy parameter of a cubic equation of <br> state |
| :--- | :--- |
| AARD | absolute average relative deviation <br> co-volume of a cubic equation of state |
| b | second virial coefficient <br> B |
| c | speed of light in vacuum $[\mathrm{m} / \mathrm{s}]$ |
| $\tilde{A}_{1}, \dot{B}, \dot{C}$ | Antoine equation parameters |
| $\mathrm{A}_{\mathrm{s}}$ | dispersion constant $\left[\mathrm{J} . \mathrm{cm}^{6} /\right.$ molecule $\left.^{2}\right]$ |
| d | molecular diameter $[\dot{A}]$ |
| EOS | equation of state |
| f | fugacity |


| i, j | components $\mathrm{i}, \mathrm{j}$ |
| :---: | :---: |
| $\mathrm{k}_{\mathrm{ij}}, \mathrm{l}_{\mathrm{ij}}, \mathrm{m}_{\mathrm{ij}}$ | interaction coefficients between components of $i$ and $j$ |
| m | parameter in Eq. (10) |
| m' | rest mass of electron [ kg ] |
| M | molecular weight |
| n | refractive index |
| N | number of experimental points |
| $\mathrm{N}_{\text {A }}$ | avogadro's number [molecule $/ \mathrm{mol}$ ] |
| $\mathrm{N}_{\text {S }}$ | number of solid molecules/surface unit |
| P | pressure [bar] |
| $\mathrm{P}_{\mathrm{C}}$ | critical pressure [bar] |
| PR | Peng-Robinson equation of state |
| Q | fitting parameter $\left[\mathrm{m}^{3}\right]$ |
| R | universal gas constant |
| p, q, r, $\hat{K}, \hat{L}$ | parameters in Eqs. $(26,27)$ |
| SRK | Soave-Redlich-Kwong equation of state |
| T | temperature [K] |
| T ${ }_{\text {c }}$ | critical temperature [K] |
| Tr | reduced temperature |
| U, W | parameters in Eq.(6) |
| $\mathrm{y}_{\mathrm{i}}$ | mole fraction of component $i$ in the supercritical phase |
| Z | intermolecular distance between $\mathrm{CO}_{2}$ and solid molecule |
| Z | compressibility factor |

## Greek symbols

| v | molar volume [liter $\mathrm{mol}^{-1}$ ] |
| :---: | :---: |
| $\phi$ | fugacity coefficient |
| $\omega$ | acentric factor |
| $\sigma$ | intermolecular distance at zero-interaction energy [ $\dot{A}$ ] |
| $\alpha$ | parameter in Eq. (9) |
| $\alpha_{\text {A }}, \alpha_{\text {S }}$ | polarizabilities of $\mathrm{CO}_{2}$ and solid $\left[\mathrm{cm}^{3} /\right.$ molecule] |
| $\chi$ | magnetic susceptibility [ $\mathrm{cm}^{3} /$ molecule] |
| $\varepsilon$ | potential energy interaction $\left[10^{32} \mathrm{~J} / \mathrm{mol}-\right.$ ecule] |
| $\rho$ | absolute density |
| Superscripts |  |
| exp | experimental |
| calc | calculation |
| s | solid phase |
| sat | saturation |

## CONCLUSION

In the current work, the cubic Peng-Robinson (PR) and Soave-Redlich-Kwong (SRK) equations of state have been used to estimate the solid solubilities of 18 solutes in supercritical carbon dioxide by using four mixing rules called the van der Waals one fluid rule with one (VDW1) and two (VDW2) adjustable parameters, the covolume dependent (CVD) rule and the new mixing rule. Furthermore, the optimized adjustable parameters of the new mixing rule are reported for 665 experimental data points. The prediction of the new mixing rule model for solid solubility calculations in supercritical carbon dioxide is more accurate than the other mixing rules in the same equations of state.

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[^0]:    -Cal.2,5-Xyleno
    —Cal.Benzoin
    -Cal.3,4-Xylenol
    -Cal.Fluorene
    Cal.Mandelic Acid
    -Cal.Naphthalene
    Cal.Pyrene
    -Cal.Propyl-4-hydroxy benzoate

    - Exp.2,5-Xylenol
    * Exp.Benzoin
    - Exp.3,4-Xylenol
    + Exp.Fluorene
    - Exp.Mandelic Acid
    - Exp.Naphthalene
    $\times$ Exp.Pyrene
    Exp.Propyl-4-hydroxy benzoate

